

National Institute for Land and Infrastructure Management Ministry of Land, Infrastructure, Transport and Tourism Asahi1, Tsukuba-shi, Ibaraki, 305-0804, Japan

INTRODUCTION OF ROAD TECNOLOGY AND POLICY MAKING - International Joint Seminar of VJU and NILIM -

November 25th, 2022

- On November 25th, 2022, NILIM held the International Joint Seminar online with VJU*, Hanoi.
- The theme of this seminar is "Introduction of Road Technology and Policy Making". NILIM presented our technologies about maintenance and management of road structures, disaster prevention and recovery, and policies of MLIT. VJU presented characteristics of soft clays in the red river delta.
- To begin with, the Director-General of NILIM and Program Director of VJU delivered greetings as organizers. Next, there were presentations and Q&A sessions and the seminar concluded with a successful address from VJU at last.
- The following is the outline and activities of the seminar. For the details, please see the next page and beyond.

* Vietnam Japan University was established in Hanoi in 2014 by JICA's Technical Cooperation Project. VJU has tried to develop human resources practically on an international level by conducting internships at Japanese companies. Japanese language is also taught as a required subject. VJU has been offering only Master's Courses but they also opened Undergraduate Courses in September, 2022.

1. TIME

November 25th, 2022 (Fri) 13:00-15:20 (Vietnam Time) 15:00-17:20 (Japan Time)

2. OUTLINE

• Title

Introduction of Road Technology and Policy Making

Attendees

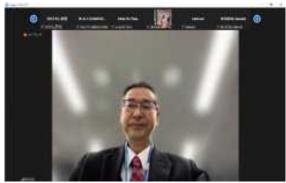
96 (Number of pre-registrations), including 14 from Japanese companies

• Venue

Online (ZOOM)

• Contents

At the beginning, the Director-General of NILIM gave an opening address as the organizer and the Director for International Affairs, Planning Division, Road Bureau, MLIT addressed as the guest of honor. Then, the Road Structures Department gave a presentation on "Maintenance and Management of Road Structures in Japan", the Road Traffic Department presented on "Efforts to Identify Passable Roads after Disasters from Road Traffic Big Data", and the Sabo Department presented on "Prevention and Mitigation of Sediment Disasters in Japan". VJU presented on "Compressibility Characteristics of Soft Clays in the Red River Delta". There were vigorous Q&A sessions in each presentation. The joint seminar finished in great success with closing remarks by a lecturer from VJU.



Greeting by Director-General of NILIM



Commemorative screenshot of attendees



Participants of NILIM



INTRODUCTION OF ROAD TECHNOLOGY AND POLICY MAKING

-International Joint Seminar of VJU and NILIM-

•TIME

25th Nov 2022 (Fri) 13:00-15:20 (Vietnam Time) 15:00-17:20 (Japan Time)

VENUE

Online(ZOOM)

REGISTRATION AND CONTACT INFO

Email:takeda.s@vju.ac.vn Register: https://forms.gle/oiMq Yu7oQd6MHxCh6



PROGRAM

- 1. Opening address & Guest's address
- 2.Session
 - (1) Maintenance and management of road structures in Japan: Decade of road maintenance revolution
 - (2) Efforts to identify passable roads after disasters from road traffic big data
 - (3) Prevention and mitigation of sediment disasters in Japan
 - (4) Compressibility Characteristics of Soft Clays in the Red River Delta

3.Closing

TIME TABLE

■13:00~13:10 (Vietnam Time), 15:00~15:10 (Japan Time) Opening Address

- Mr. OKUMURA Yasuhiro, Director-General, National Institute for Land and Infrastructure Management (NILIM), Ministry of Land, Infrastructure, Transport and Tourism, Japan
- Prof.Dr. Sc. Nguyen Dinh Duc, Program Director, Master's Program in CIVIL Engineering(MCE), VNU Vietnam Japan University (VJU), (Affiliation: Vietnam National University (VNU), Hanoi)

■13:10~13:15 (Vietnam Time), 15:10~15:15 (Japan Time) Guest's Address

• Mr. FUKUI Takanori, Director for International Affairs, Planning Division, Road Bureau, Ministry of Land, Infrastructure, Transport and Tourism, Japan

■13:15~15:15 (Vietnam Time), 15:15~17:15 (Japan Time)

Session1: Maintenance and management of road structures in Japan: Decade of road maintenance revolution

Dr. KATAOKA Shojiro (Research Coordinator for Road Structures Management, Road Structures Department, NILIM)

Session2: Efforts to identify passable roads after disasters from road traffic big data

Mr. ISHIHARA Masaaki (Researcher, Intelligent Transport Systems Division, Road Traffic Department, NILIM)

Session3: Prevention and mitigation of sediment disasters in Japan

Dr. AKIYAMA Kazuya (Research Coordinator for Sediment Disaster Prevention, Sabo Department, NILIM)

Session4: Compressibility Characteristics of Soft Clays in the Red River Delta Ms. Khin Phyu Sin (Master's Program in CIVIL Engineering(MCE), VNU Vietnam Japan University (VJU))

■15:15~15:20 (Vietnam Time), 17:15~17:20 (Japan Time) Closing

• Dr. Nguyen Ngoc Vinh, Lecturer, Master's Program in CIVIL Engineering(MCE), VNU Vietnam Japan University (VJU)

Chairman: Dr. Nguyen Tien Dung, Lecturer, Master's Program in CIVIL Engineering(MCE), VNU Vietnam Japan University (VJU)



Maintenance and Management of

Road Structures in Japan:

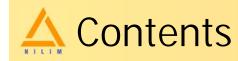
Decade of Road Maintenance Revolution

KATAOKA Shojiro

Research Coordinator for Road Structures Management

Road Structures Department, NILIM, MLIT, Japan

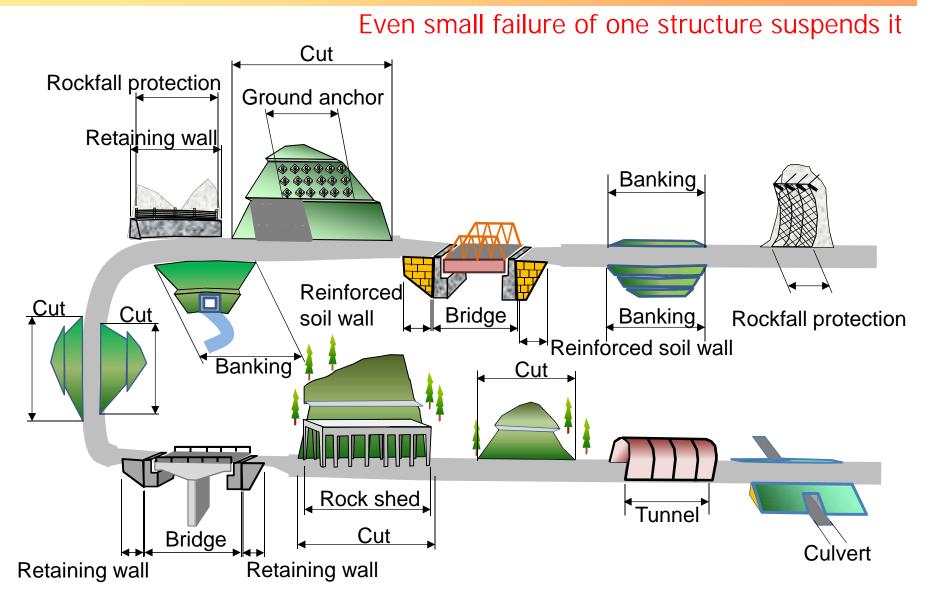
VJU-NILIM Joint Seminar online, November 25, 2022



- 1. Introduction
- 2. Decade of Revolution from 2012
- 3. Contribution & Challenge by NILIM

1

A Various structures support road traffic



A Road structures suffer deterioration

In Japan, we have...

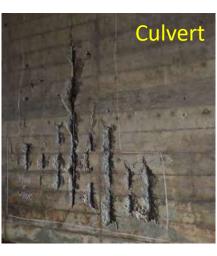


700K+ Bridges



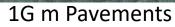
10K Tunnels





Various types of Earthworks

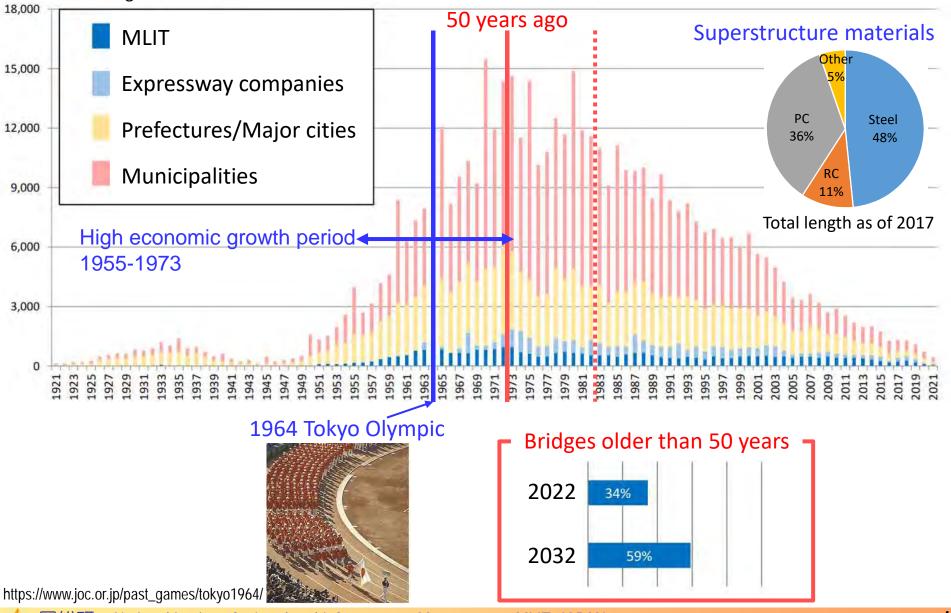






… because they are aging.

Number of bridges built



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A History of national highway inspection (-2012)

Each Regional Bureau used its own guideline

 \rightarrow Uneven inspection methods and results

1988 First common Bridge Inspection Guideline

→Close visual inspection of each bridge every 10 years

Serious deterioration cases were found



2001 NILIM was established and started supporting revision of the guideline

2004 Revised Bridge Inspection Guideline

- \rightarrow Close visual inspection every 5 years
- \rightarrow "Evaluation" was introduced for taking action

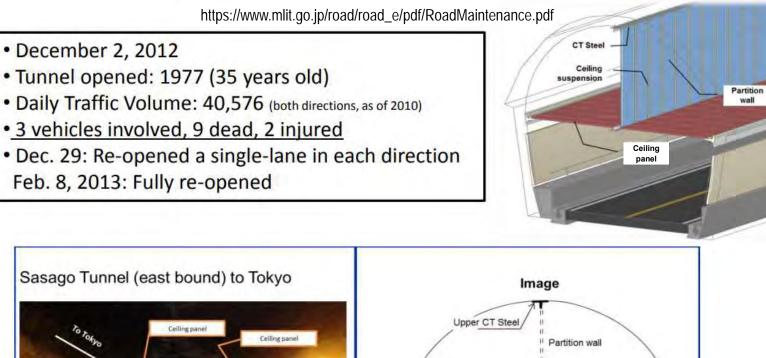
	Good
II	Preventive maintenance
	Repair work is required
IV	Emergency action is needed

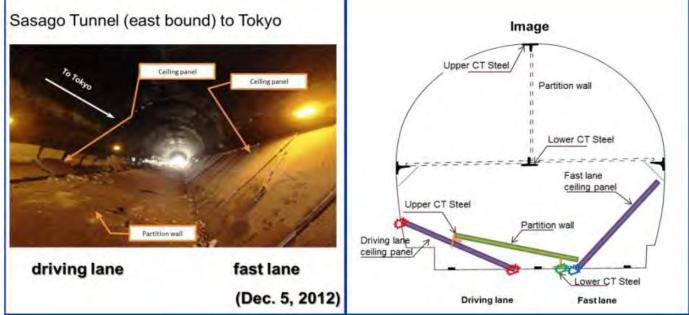
2012 Ceiling panel collapse in Sasago Tunnel



Dec 2, 2012

A Turning Point : Ceiling panel collapse in Sasago tunnel



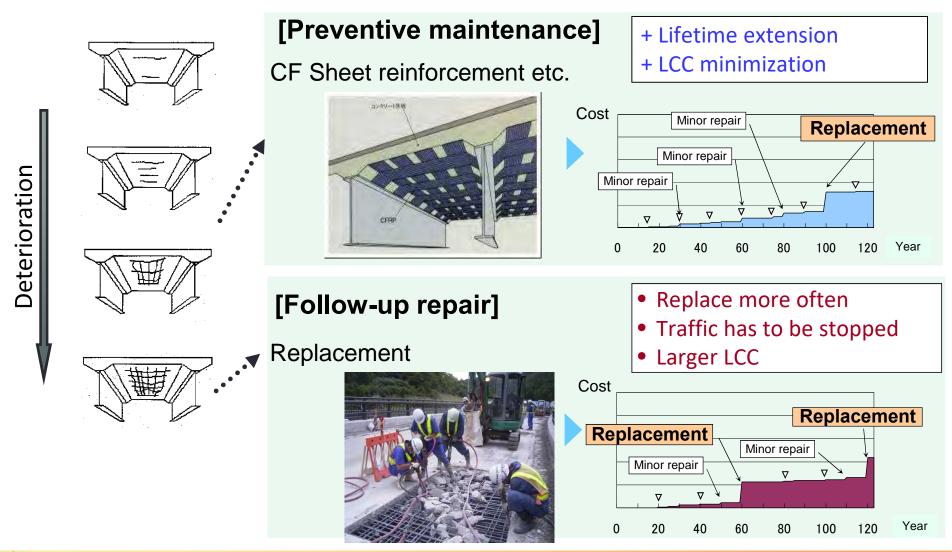


NILIM supported verification of inspection method and the accident analysis.

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A Future Direction : Preventive Maintenance

Repeat minor maintenance work for saving life cycle cost compared to leaving the damage until replacement or major repair work.



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Decade of revolution from 2012 (1/3)

2012 Ceiling panel collapse in Sasago Tunnel

2012 Urgent inspection for tunnel equipment

2013 Intensive inspection for road stocks

We must

- establish a maintenance cycle
 - (obligation of administrators)
- establish a mechanism to facilitate the cycle (budget, system, skill, support)

2013.6 Amendment of Road Act

2014.3 Public notice of revision to Ordinances

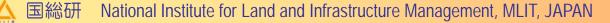
2014.7 into force

 \rightarrow Implement a close visual inspection of all tunnels, bridges, etc. every five years

 \rightarrow Evaluate structure condition across Japan based on a uniform standard

2014.6 National guidelines for periodic inspection

NILIM contributed to the revisions and draft-making of the guideline.

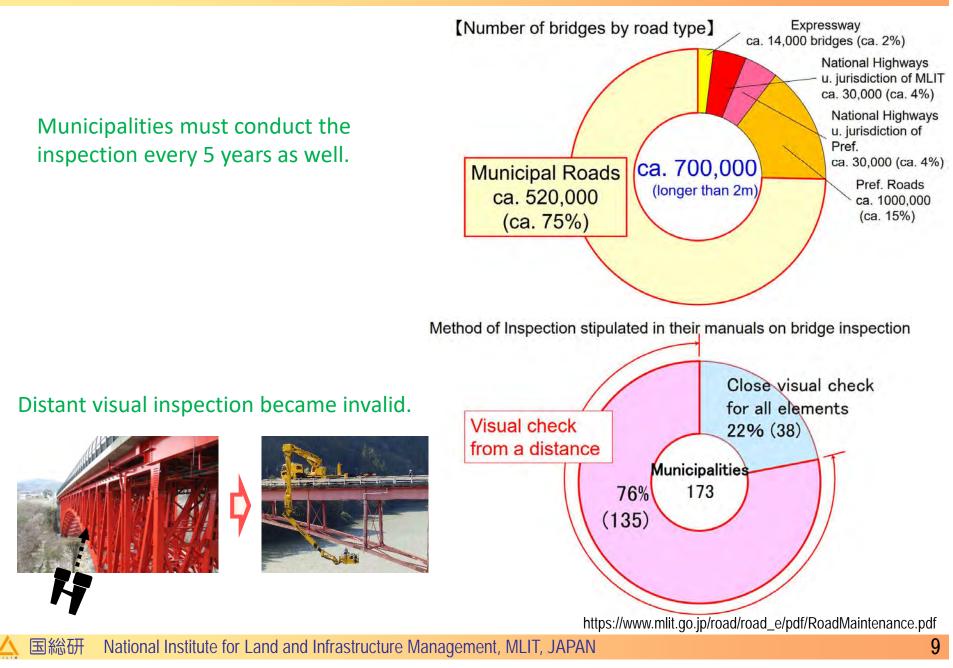






Close visual inspection of tunnel equipment and bridge

A Dramatic changes in inspection



A 2014 National guidelines for periodic inspection

MLIT, with support from NILIM, developed a series of inspection guidelines describing

- Types of deformation need attention
- Case examples

in order to assist inspection by municipalities .

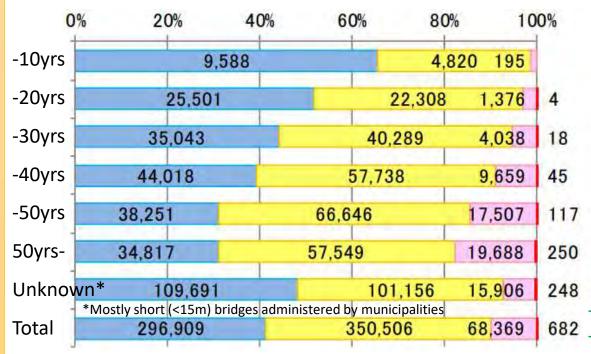




\triangle Decade of revolution from 2012 (2/3)

2014.6 National guidelines for periodic inspection

2014.7 First round of the periodic inspection started (-FY2018)



Summary of the first round inspection(bridges)

I	Good
<mark>-</mark> 1	Preventive maintenance
ш	Repair work
■ IV	Emergency action

Older bridges are worse, as expected.
Quantitative evidence was obtained for planning maintenance strategy.

2019.2 Revised national guidelines for periodic inspection

NILIM contributed to the revisions and draft-making.

A 2019 National guidelines for periodic inspection

Issues from the 1st-round inspection (FY2014-2018)

- Difficult :

Inspections require technical considerations

 \rightarrow Reference materials

 \checkmark Reference for checking underwater part



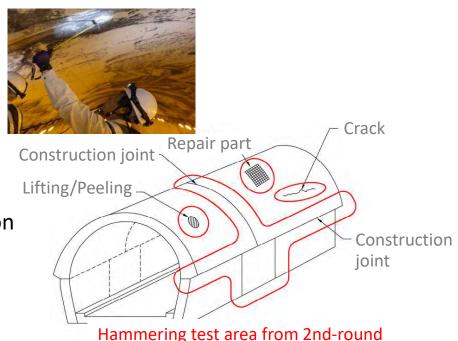
- ✓ Reference for damage examples and inspection of bridges with tensile elements (Suspension, Cable-stayed, Arch,)
- Consuming:

Prevent over-checking

→ Illustrate necessary/unnecessary checking in the guidelines or references

Cost-cut by new technology

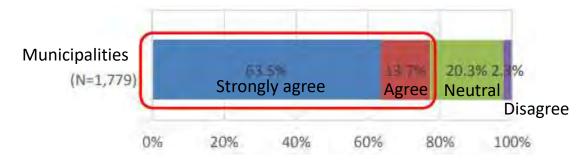
 \rightarrow Alternative method to close visual inspection



Support for using new technologies

Questionnaire to municipalities:

The cost required for the inspection is a burden.



\rightarrow Strong needs for cost-cut by new technologies



- \rightarrow What technologies are available?
- \rightarrow Performance catalog of inspection support technologies

16 items (Feb. 2019) \rightarrow 172 items (Sep. 2022)

 \rightarrow Guideline & Examples

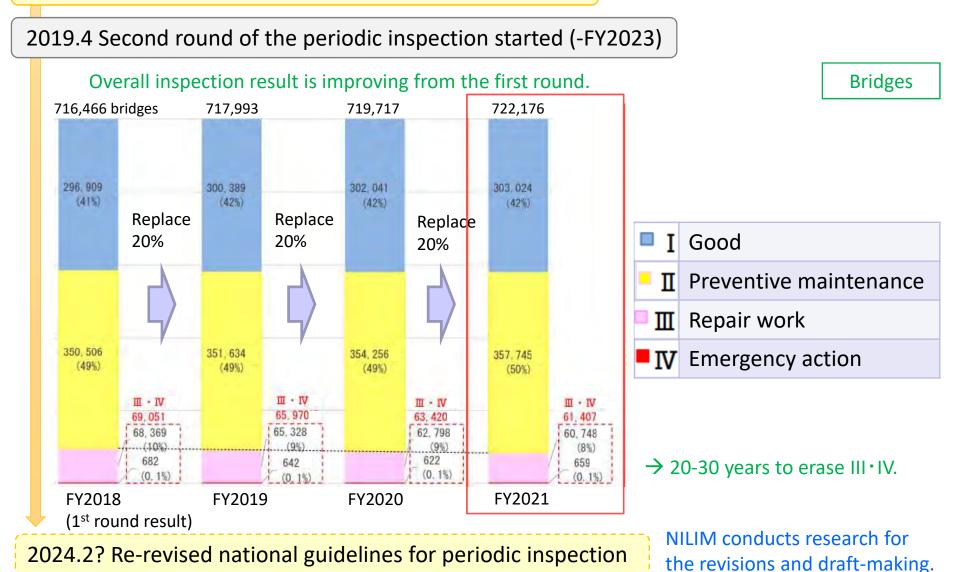
National Institute for Land and Infrastructure Management, MLIT, JAPAN 国総研

An example (one item)

https://www.mlit.go.jp/road/sisaku/inspection-support/

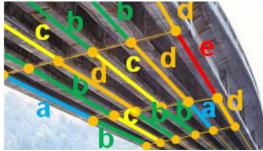
A Decade of revolution from 2012 (3/3)

2019.2 Revised national guidelines for periodic inspection



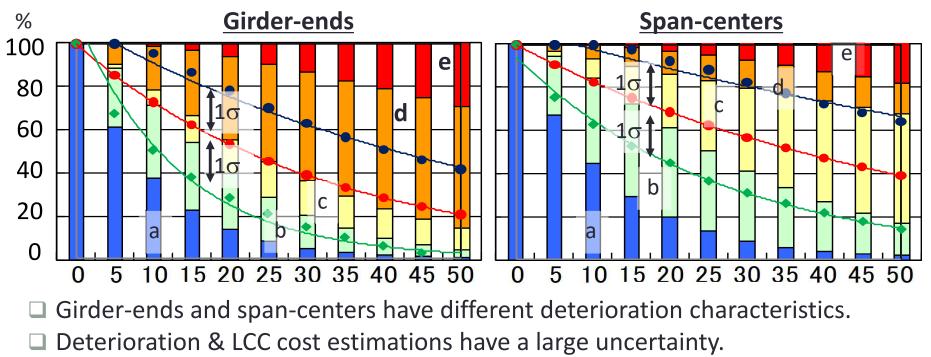
Contribution & Challenge by NILIM (1/2)

NILIM carried out stochastic analysis using segment-level inspection data of 24,000 bridges.



a-e: Damage extent of segment

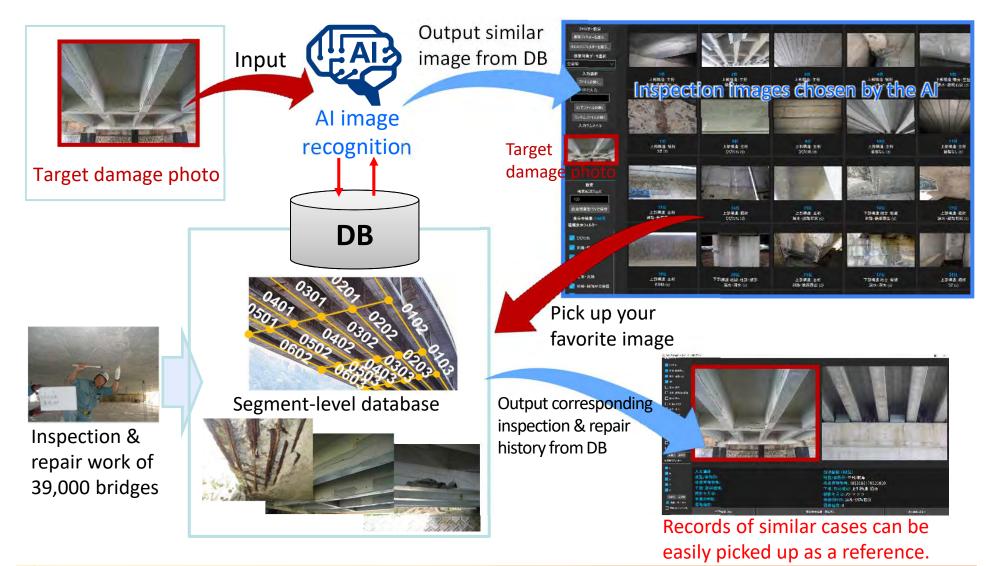
Example: Markov chain state transition probabilities for corrosion in steel I-girder beams



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Contribution & Challenge by NILIM (2/2)

NILIM developed "AI image-searching application" for convenient use of inspection big data.





- Learning precious lessons from the tunnel accident in 2012, periodic inspection was regulated to all road administrators and has been conducted since 2014.
- Overall inspection result seems improving but still takes a few decades to change our major work from "follow-up repair" to "preventive maintenance".
- Administrators, especially those in municipalities, feel the inspection cost is heavy and cost-cut by new technologies becomes an urgent issue.
- MLIT continues support for using new technologies.

A Thank you for your kind attention !

For more about NILIM...

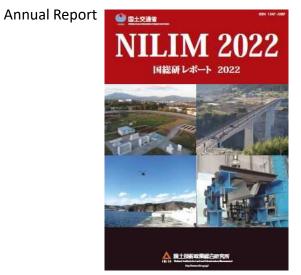


NILIM Website (English) http://www.nilim.go.jp/english/eindex.htm

You Tube Channel https://www.youtube.com/channel/UC5I193hxIF1CrZ85DTBnm8Q



http://www.nilim.go.jp/english/about/nilim2022e.pdf



http://www.nilim.go.jp/english/annual/annual2022/ar2022e.html



2022 International Joint Seminar of VJU and NILIM

Efforts to Identify Passable Roads after Disasters from Road Traffic Big Data

Researcher, Intelligent Transport Systems Division, Road Traffic Department, NILIM, Japan

ISHIHARA Masaaki

1. Introduction

2. Traffic Record Display System

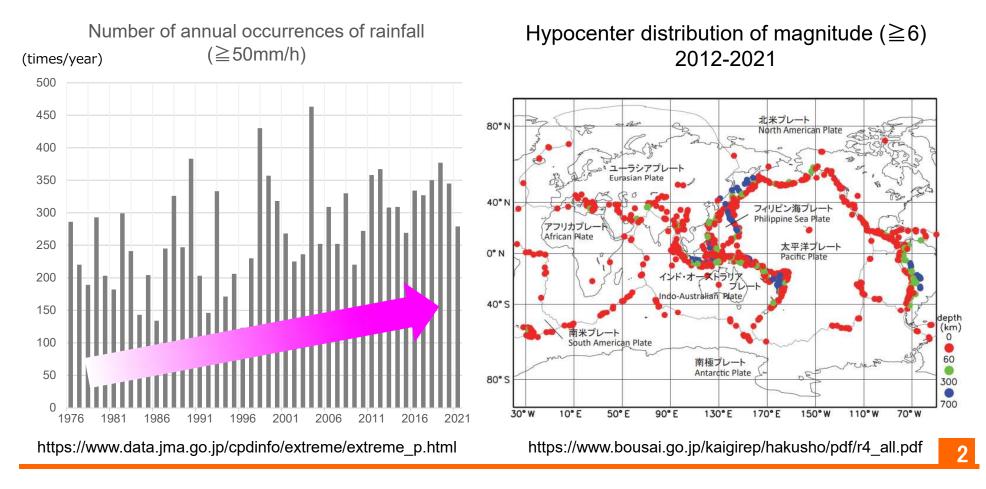
- 2.1 Outline
- 2.2 Issues & Improvements

3. Example of applying the system

4. Conclusion

1. Introduction

- In Japan, flood damage has become more severe, and the danger of large-scale earthquakes is increasing.
- In the event of a disaster, it is necessary to provide drivers with road closure information as quickly as possible.



1. Introduction

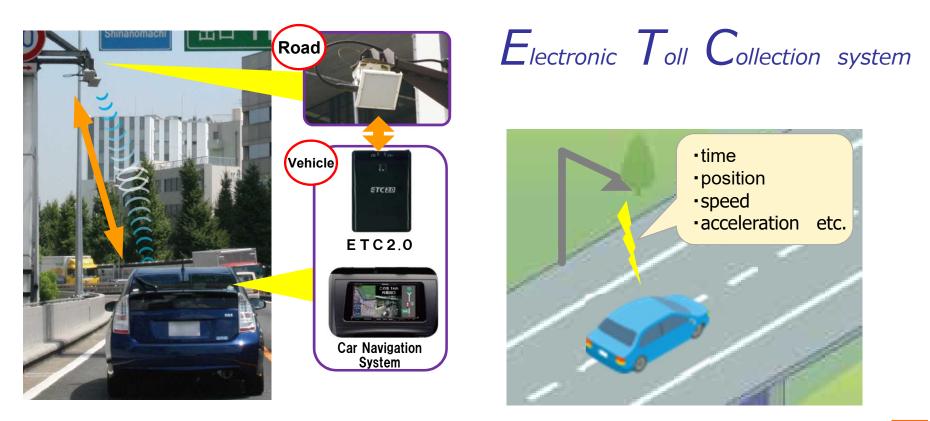
- Field studies are necessary to grasp the locations of road closures
- Lack of immediacy due to the time it takes to collect the initial information
- Demand for a system that provides road administrators with real-time information on non-passable roads and traffic



https://www.mlit.go.jp/river/sabo/jirei/r2dosha/r2_07gouu_201222.pdf

2.1 Outline

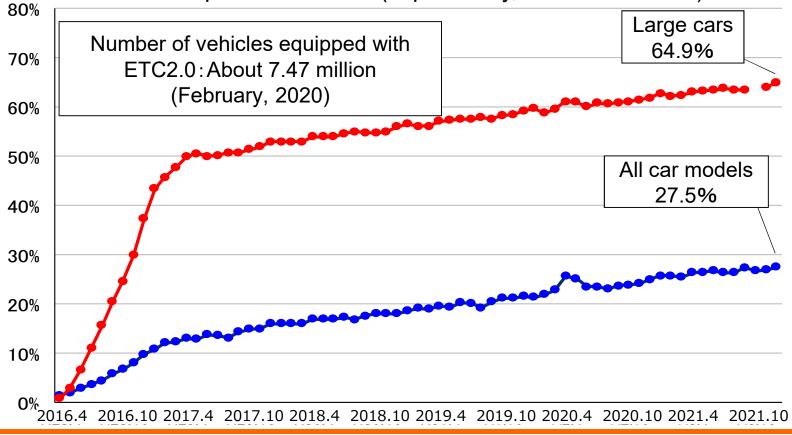
- Information overlaid on a map: traffic records derived from vehicle probe data.
- Grasp the traffic status of all roads in Japan.
- Identify passable routes that can be used to access disaster areas.



2.1 Outline

- Information overlaid on a map: traffic records derived from vehicle probe data.
- Grasp the traffic status of all roads in Japan.
- Identify passable routes that can be used to access disaster areas.

ETC2.0 penetration rate (expressway, December 2021)



2.2 Issues & Improvements

Issues

- Lacking in terms of immediacy of data
- Adapting to big data
- Difficulty comparing with past data
- Deterioration and obsolescence

Improvement

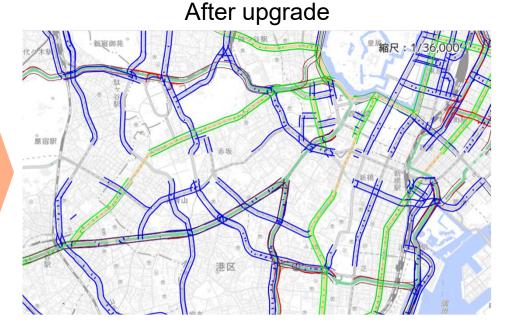
- I. Display the traffic record
- II. Segmented display by road type
- III. Immediacy of data
- IV. Displayable time frame

I. Display the traffic record

Before upgrade



- Display roads traveled by one or more vehicles on a map
- Display content cannot be adjusted according to conditions



Free settings can be made according to traffic conditions and regions

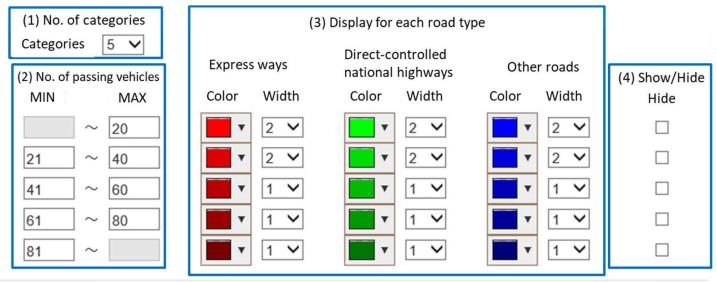
I . Display the traffic record

Improved to display the number of passing vehicles classified by category

- (1) Number of categories displayed
- (2) Classification by number of passing vehicles
- (3) Display for each road type

(color and width of displayed lines)

(4) Lines can be shown or hidden



Example display settings for number of passing vehicles

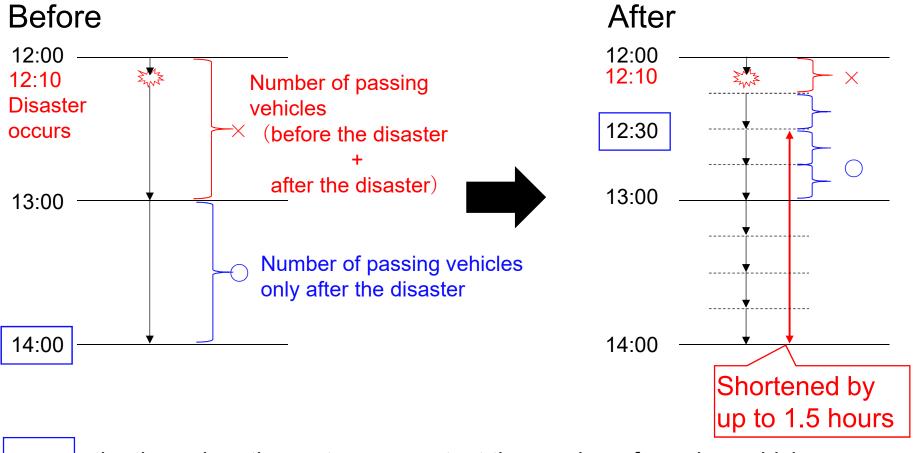
II . Segmented display by road type

- Before the upgrade, the system would display traffic records on the map by road type in two categories.
- Because road type is not segmented, jurisdiction of the road administrator cannot be determined on the map.
- Improved the system to allow for segmented display by road type.



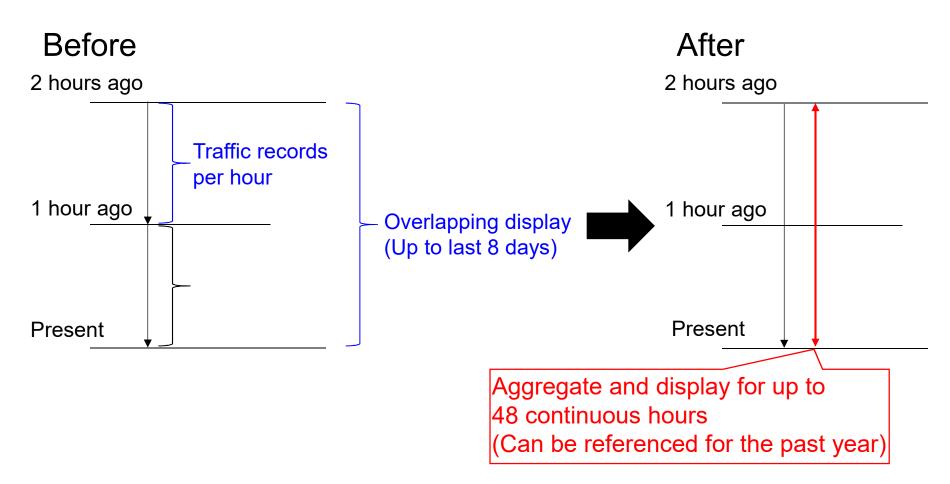
Example of display by road type

III. Immediacy of data



: the time when the system can output the number of passing vehicles after the disaster

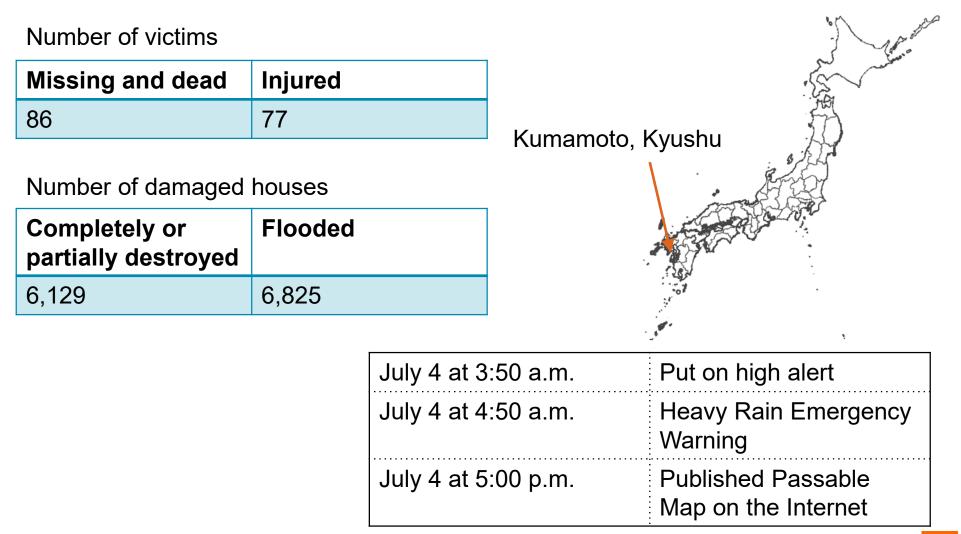
IV. Displayable time frame



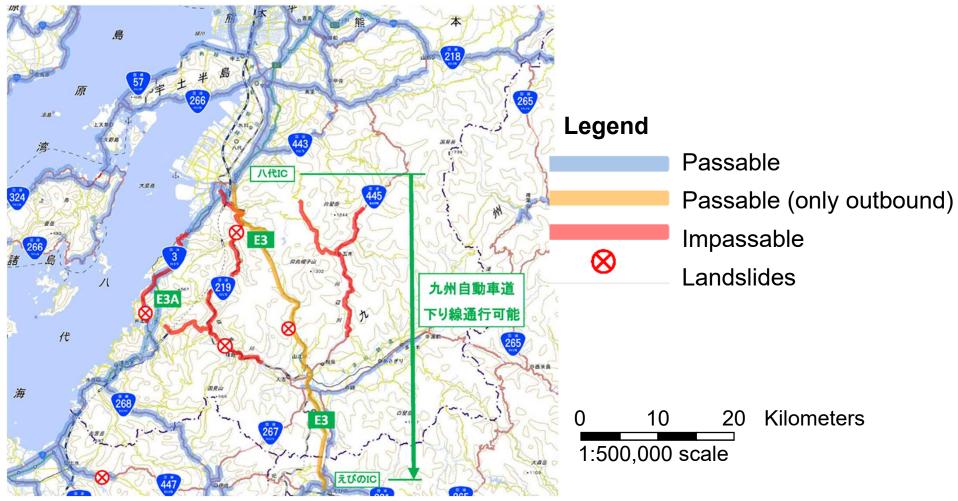
Upgrade of displayable time frame

3. Application Examples

About the 2020 Kyushu Floods



3. Application Examples



The publicly available Passable Map (first version)

- System utilizes vehicle probe data collected by MLIT
- System aggregates and visualizes traffic records
- Road administrators can promptly grasp traffic restrictions
- Possible to promptly provide road users with information

In the future

- Gain an understanding of the needs and opinions of users
- Evaluate the system
- Implement function improvements

Prevention and mitigation of sediment disasters in Japan

Kazuya AKIYAMA

Research Coordinator for Sediment Disaster Prevention, Sabo Department, NILIM

Contents

 Sediment disasters in Japan
 Non structural measures (Land-use regulation and control)

1. Sediment disasters in Japan

What is sediment disasters?

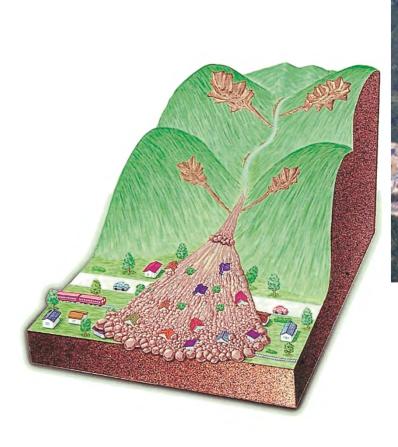
Sediment disasters can be generally classified in a debris flow, a landslide, and a slope failure



Others : Disasters or phenomena supported by Sabo (Sediment disaster prevention) Works

- Drainage sediment control: prevent sediment from flowing downstream and rising river bed
- Driftwood disaster: prevent fallen trees from flowing downstream
- Snow avalanche: avalanches damage to community
- Volcanic eruption: volcanic mud flow, debris flow, etc.

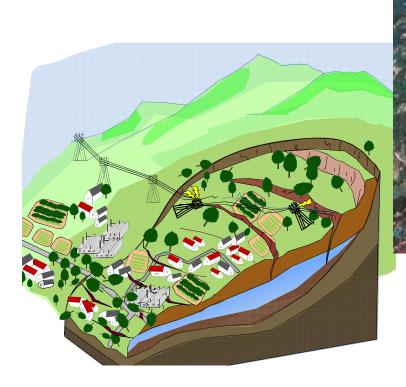
Debris flow





Part of soil, stone and gravel making up a hillside and river bed is intermingled with water from long-continuing or localized rainfall, etc. and is carried instantly downstream. The flow is called a "debris flow". The velocity being 20-40 km/hour depending on the magnitude, the debris flow easily destroy houses and other structures all at once.

Landslide





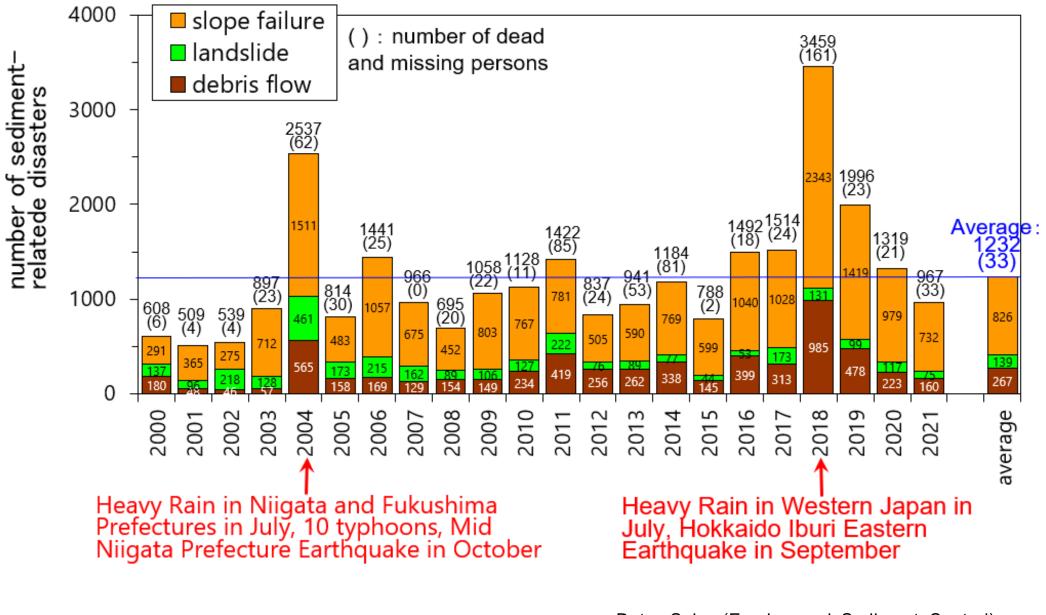
A landslide is a phenomenon in which soil mass on a slope moves slowly along the slip surface downward the slope under the influence of ground water and other causes. Since landslides occur over an extensive area and a large amount of soil mass is moved in general, it can cause serious damages.

Slope failure



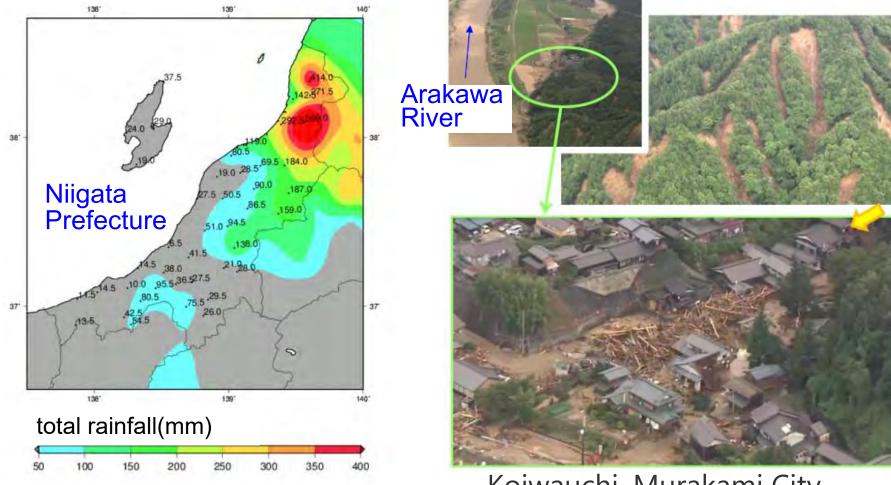
A slope failure is a phenomenon that a slope collapses abruptly due to weakened self-retainability of the earth under the influence of a rainfall or an earthquake. Because of sudden collapse of slope, many people fail to escape from it if it occurs near a residential area, thus resulting in a higher rate of fatalities.

Outline of sediment disasters from 2000 to 2021 (for 22 years) in Japan



Data: Sabo (Erosion and Sediment Control) Department, Ministry of Land, Infrastructure, Transport and Tourism (MLIT)

Sediment disasters caused by the heavy rain from August 3 to 5, 2022



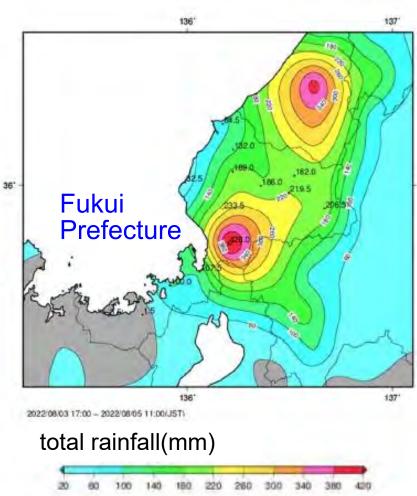
Koiwauchi, Murakami City, Niigata Prefecture

Figure : Japan Meteorological Agency(JMA)

Photos: Sabo (Erosion and Sediment Control) Department MLIT

Debris flow and driftwood disasters in the eastern part of Murakami City, Niigata Prefecture

Sediment disasters caused by the heavy rain from August 3 to 5, 2022





National Road No.8

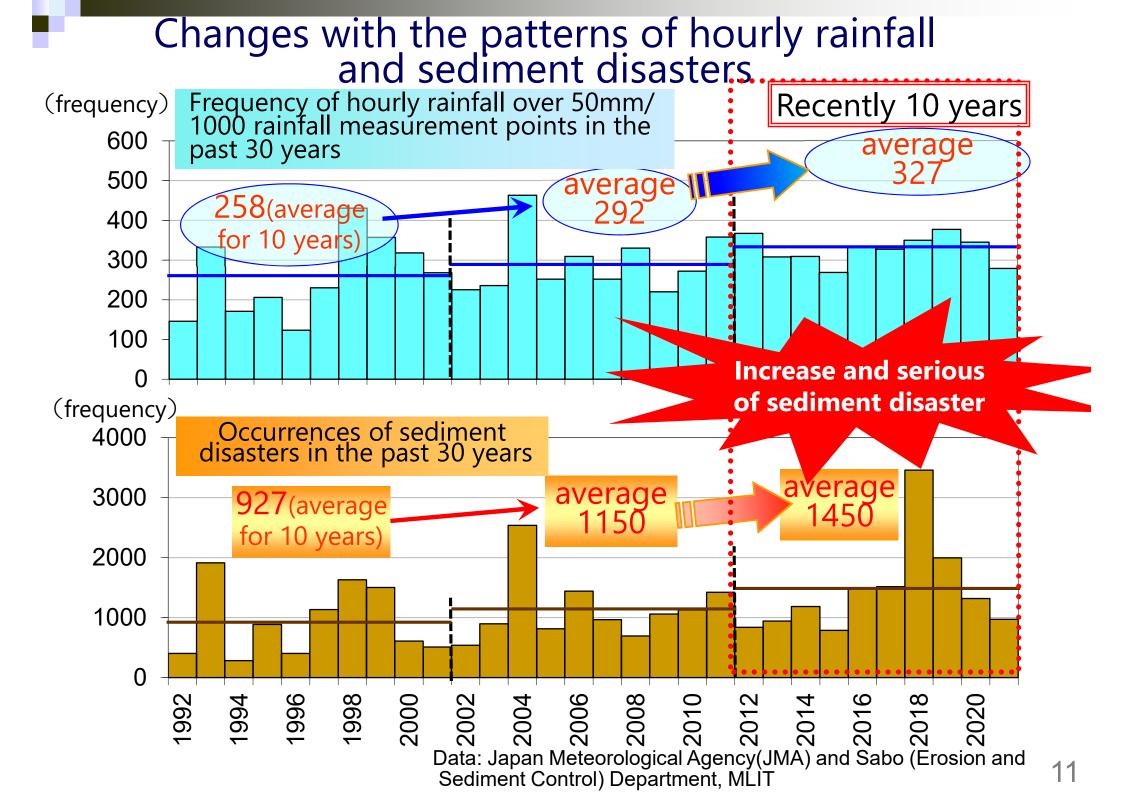


Hokuriku Expressway

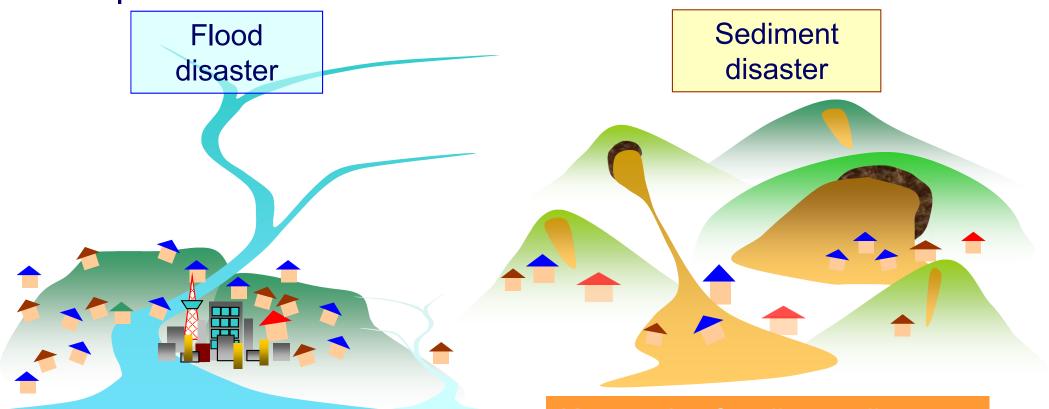
Figure : Japan Meteorological Agency(JMA)

Photos: Explanatory materials for the 3rd meeting, Fukui Prefectural Disaster Traffic Management Study Group, Kinki Regional Development Bureau, MLIT

Debris flow disasters in Minamiechizen Town, Fukui Prefecture



Comparison of flood disaster and sediment disaster



Keywords of flood disaster

- 1. Flood points exist inside river (flood area can be fixed)
- 2. Basic and trigger factors are limited (rain)
- 3. Sufficient period of time to evacuate (ex. rain \rightarrow rising river water \rightarrow disaster)
- 4. Water of rising river can be recognized and danger degree can be judged

Keywords of sediment disasters

1. Sediment disaster points exist everywhere on slope

Basic and trigger factors are various (rain, rising groundwater level, earthquake, geomorphology, geology, etc.)
 Unpredictable (sudden) phenomena (ex. earthquake→slope failure, rain→debris flow)
 Phenomena can not be recognized because of under ground and danger degree can not be judged

2. Non structural measures (Land-use regulation and control)

Sediment Disaster Prevention Law

Three strategies for preventing sediment disasters (sabo works)

Protect people

Non-structural measures Warning and evacuation

In areas designated as "sediment disaster hazard areas" based on the Sediment Disaster Prevention Laws • Preparation of hazard maps for sediment disasters

• Strengthening of warning and evacuation system through preparation of sediment disaster warning information and their dissemination, improvement of information system, etc.

 Sediment Disaster Prevention Law

Protect people & properties

Disaster mitigation/ Land monitoring

Land conservation

Structural measures Facilities against disasters

- Sabo works
- Landslide prevention works
- Slope failure prevention works

• Sabo Law

- Landslide Prevention
 Law
- Law on Prevention of Disasters Caused by Steep Slope Failure

Control development and protect people

Non-structural measures

Restriction on acts, land development and building structure

Sabo designated area, landslide and slope failure prevention areas • Restriction on cutting tree, banking and other acts considered harmful for the conservation of land.

Special sediment disaster hazard area (Red-zone)

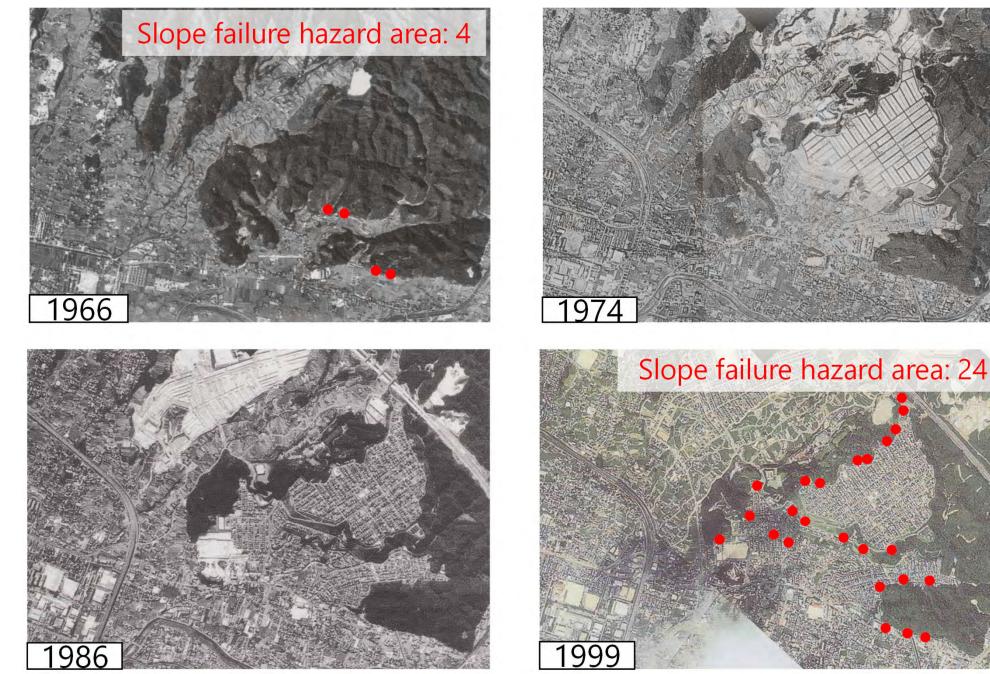
• Restriction on building structure

• Restriction on specific development works

• Sabo Law

- Landslide Prevention Law
- Law on Prevention of Disasters Caused by Steep Slope Failure
- Sediment Disaster
- Prevention Law

Urbanization and sediment disasters



Situation of residential land development in Saeki Word, Hiroshima City 15



Outline of Sediment Disaster Prevention Law

The "Sediment Disaster Prevention Law*" was established with the intention of instituting comprehensive non-structural measures to protect people from sediment disasters. These non-structural measures include public of risk information of areas prone to sediment disaster, development of warning and evacuation system, restriction on new land development for housing and other specific purposes, and promotion of relocation of existing houses (legislated on May 2000).

* Law concerning the Promotion of Sediment Disaster Prevention in Sediment Disaster Hazard Area

Sediment Disaster under the Scope of the Law: Debris flow, landslide and slope failure

Preparation of basic guidelines for preventing sediment disasters [Minister of the Land, Infrastructure, Transport and Tourism]

- Basic policies for preventing sediment disasters
- Guidelines for basic survey
- Policy in the designation of special sediment disaster hazard areas
- •Policy for relocation of buildings in special sediment disaster hazard areas

Implementation of basic survey [Prefectural government]

•Survey for designation of sediment disaster hazard areas and special sediment disaster hazard areas

Designation of sediment disaster hazard area (area prone to sediment disaster)[Governor of prefectural government]

• Establishment of a system for the communication of information, and warning and evacuation • Publicity of information on warning and evacuation to local people

Designation of special sediment disaster hazard area (area where damages to building and serious hazards may be posed to residents) [Governor of prefectural government] •License system for specific land development

- License is required for land development for housing and social welfare facilities
- Restriction on building structure (Building certification is required even for buildings outside the city planning area)
- Recommendation of relocation of buildings that are vulnerable to serious damages in case of a sediment disaster
- Financing and funding for those who move their residence to a safe area under recommendation

Implement basic survey Survey geomorphology, geology and land use of areas such as stream or slope where suffering sediment

disasters



Designate hazard area Designate areas based on the basic survey

Sediment disaster hazard area (Yellow zone)

(area prone to sediment disaster)

Special sediment disaster hazard area (Red-zone)

(area where damages to building and serious hazards may be posed to residents)

Determination of sediment disaster hazard area (Yellow Zone)

Debris flow

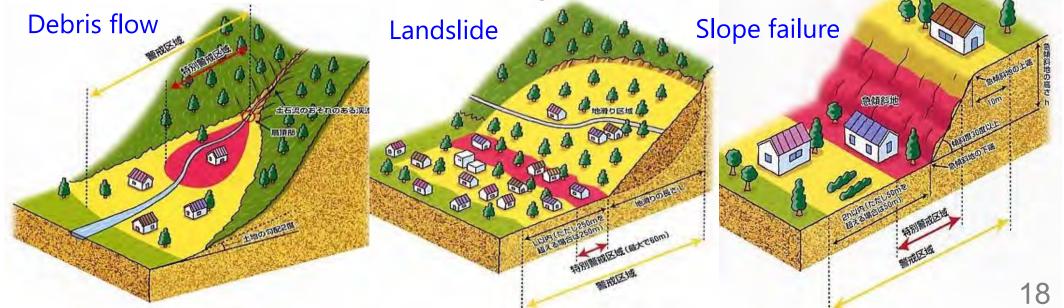
Area located under a torrent prone to debris flows and having a slope gradient 2 degrees or more below the crest of the alluvial fan.

Landslide

- Landslide area (Area which is currently prone to landslides or possibly vulnerable to landslide in future)
 Area included within a distance equivalent to the length of the landslide mass from the bottom end of the landslide area (250m if the length of the landslide mass is longer than 250m)

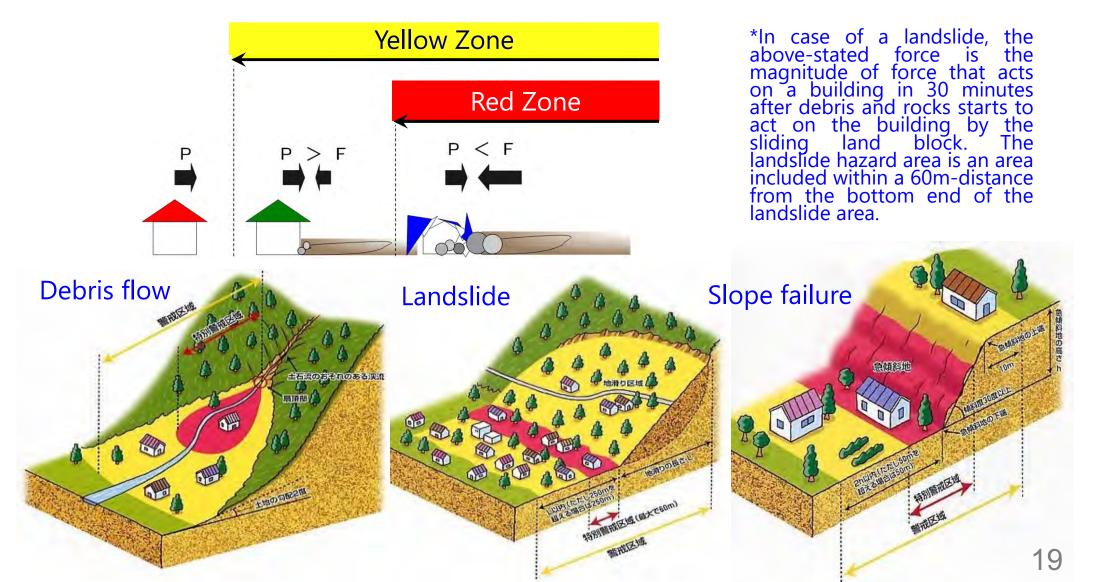
Slope failure

- Area having a slope gradient of 30 degrees or more and slope height of 5m or morĕ
- Area included within a 10m horizontal distance from the top end of the slope
- Area included within a distance twice the slope height from the bottom end of the slope (50m if the slope height is more than 50m)



Determination of special sediment disaster hazard area (Red Zone)

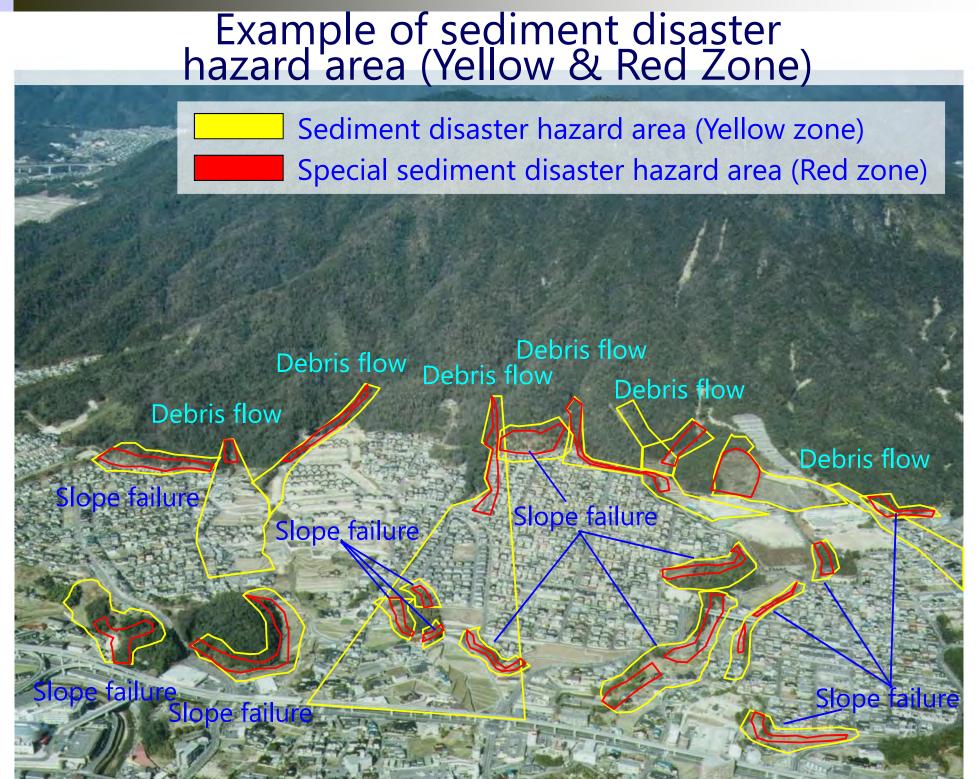
Area in which the magnitude of force exerted on a building by the movement of earth and rocks caused by slope failure exceeds the structural strength that an ordinary building can withstand without causing injury or death.



Sign board of sediment disaster hazard area (Yellow zone) and special sediment disaster hazard area (Red zone)

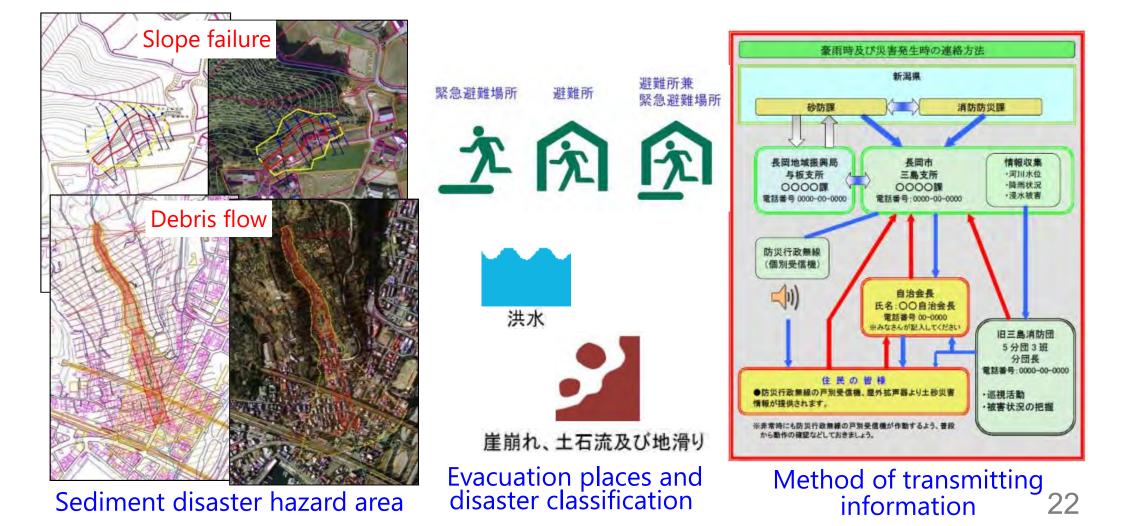




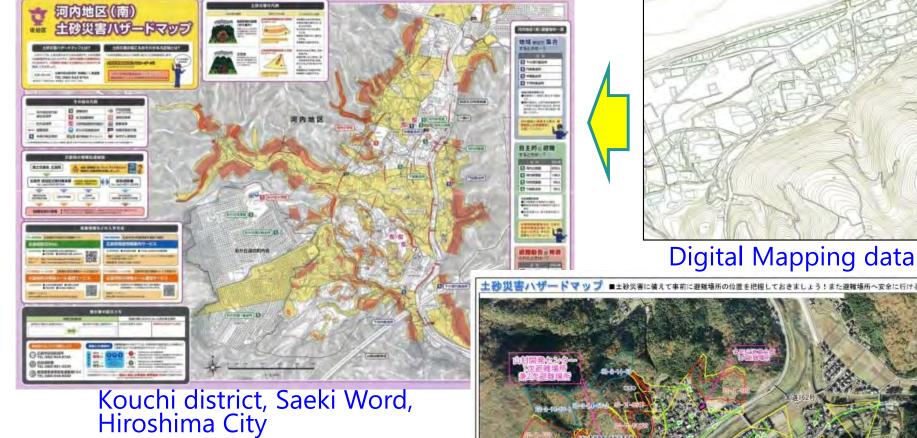


Sediment disaster hazard map

A hazard map against sediment disaster shows the relation between debris flow, landslide, and slope-failure hazard areas and evacuation places, evacuation routes, method of transmitting information at the event of sediment disaster, and necessary matters in order to ensure smooth warning and evacuation.

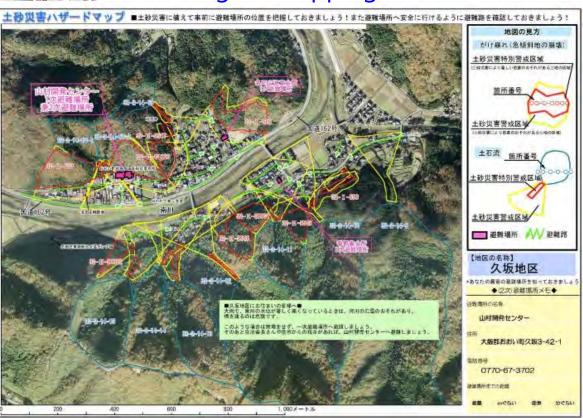


Examples of sediment disaster hazard map





Aerial photo (orthophoto)



Kusaka district, Ohi Town, Fukui Prefecture 23

Summary

Three strategies for preventing sediment disasters

- Structural measures (Facilities against disasters)
 Hard measures are important to protect people life and properties
- Non structural measures (Warning and evacuation)
 Protect people even if properties are damaged
- Non structural measures (Restriction on acts, land development building structure)
 - Do not increase hazard area

Thank you for your attention

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Compressibility Characteristics of Soft Clays in the Red River Delta

Presented by Khin Phyu Sin



Content

- 1. Introduction
- 2. Objective of the research
- 3. Methods used in this study for the determination of c_r , c_v , C_c , C_r , σ'_p
- 4. Location of the Study sites
- 5. Sample collections
- 6. Analysis results and procedure
- 7. Conclusions
- References
- Appendix

1. Introduction

Geological condition of the RRD

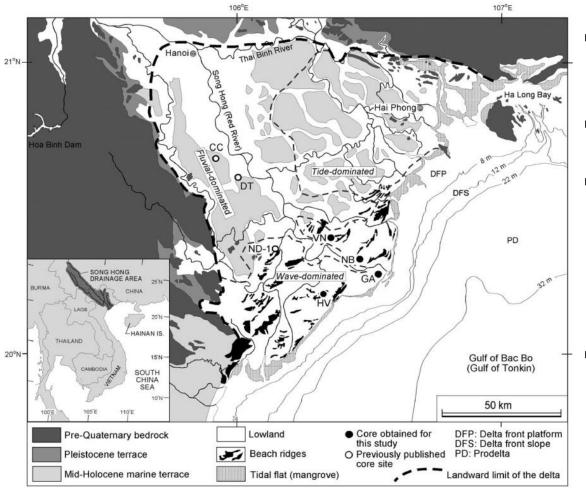
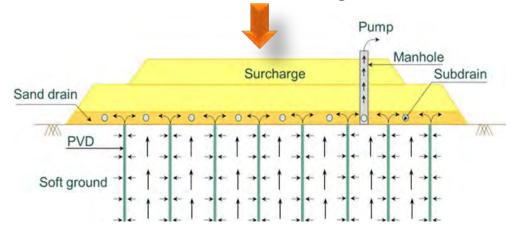


Figure 1. Quaternary geological and topographical map of RRD and adjacent areas (Tanabe et al., 2006)

- Second largest delta in Vietnam and fourth-largest delta in Southeast Asia, after the Mekong, Irrawaddy, and Chao Phraya deltas, in terms of delta plain area
- It was formed due to the sedimentation process throughout the Holocene period (9 kyr BP to date).
- Quaternary and Holocene sediments in the delta were strongly influenced by both fluvial and marine environments. Stratigraphic cross sections in the delta show the presence of fluvial sediments, estuarine sediments and deltaic sediments (Funabiki et al. 2007)
- The sediment accumulation curves (attitude vs age) from Tanabe et al., 2006 and Funabiki et al., 2007 indicate that up to the depth of about 40 m (from the present MSL), all deposits found from the cores are Holocene sediments with the age of less than 10 kyr;

1. Introduction

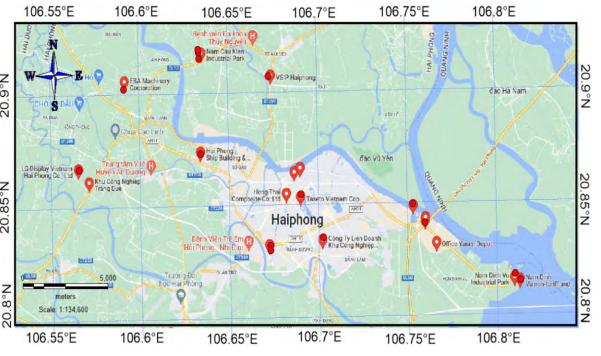
- The Red River Delta (RRD) includes many industrial zones (parks) and expressways where soft ground in large scale zones must be improved before the construction of facilities.
- Consolidation parameters, especially c_r and c_v, are important parameters in estimating ultimate and timedependence settlement values of the ground.



Excess Pore water pressure (u) at any time t after loading

 $c_r \left(\frac{\partial^2 u}{\partial r^2} + \frac{1}{r} \frac{\partial u}{\partial r} \right) + c_v \frac{\partial^2 u}{\partial z^2} = \frac{\partial u}{\partial t} \quad \text{Eq. 1.} \quad \text{where } c_r \text{ and } c_v = \text{horizontal and vertical coefficients of consolidation of soil}$ Settlement of the improved ground at any time t

$$S_t = U_t S_c = \left(1 - \frac{u}{u_0}\right) S_c = f(c_r, c_v, t, S_c) \leftarrow \text{Eq. 2.}$$
 where $S_c = \text{ultimate consolidation settlement}$



Many industrial Zones in Hai Phong City (similar to other provinces in the delta)

2. Objectives of the Research

To evaluate horizontal coefficient of consolidation from consolidation test with central drain (e.g., $c_{r,CD}$) and with a peripheral drain (e.g., $c_{r,PD}$) of clays at some test sites in the delta using existing methods and to rank the reliability of the methods.

> To examine the $c_{r,PD}/c_{r,CD}$ ratios from analytical solution on ideal soil and from experimental data on actual soil and the influence of some parameters to the ratios.

> > To evaluate compression index (C_c), recompression index (C_r) and preconsolidation stress (σ'_p) of the clays from the test sites and develop possible correlations for the parameters.

3. Methods used in this study for the determination of c_r , c_v , C_c , C_r , and σ'_p

Methods to determine radial coefficient of consolidation, c_r , vertical coefficient of consolidation, c_v , compression index (C_c), recompression index (C_r) and preconsolidation stress (σ'_p) from Oedometer test

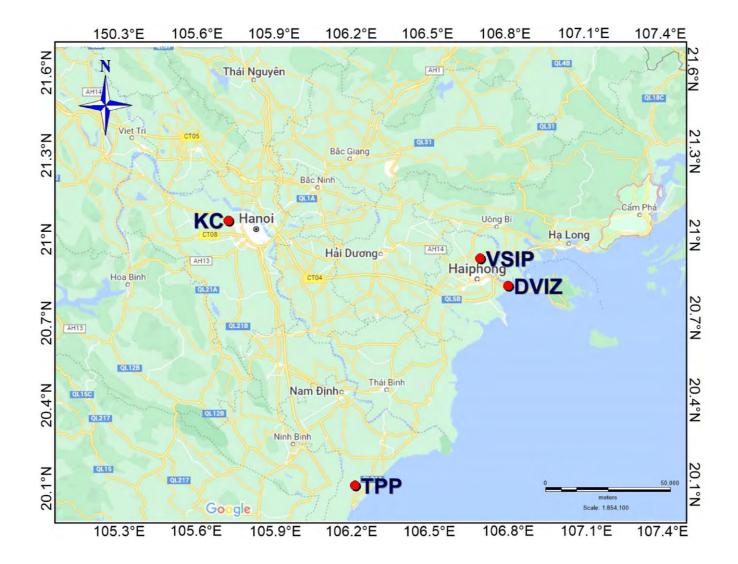
Table 1. Existing methods for the determination of c_r from radial consolidation test with a CD using incremental loading		Table 2. Existing methods for determination of c_r from radial consolidation test with a PD using incremental	
1	Root t method	loading	
	(Berry & Wilkinson, 1969; Sridharan et al., 1996)	1.	Root t method (Head and Epps, 1986)
2.	Matching log(d _e ² /t) vs. U _r method (Sridharan et al. 1996)		 Inflection point method (Ganesalingam et al., 2013)
3.	Inflection point method (Robinson, 1997)		
4.	Non-graphical matching method (Robinson & Allam, 1998)	3.	Full-match method (Chung et al., 2019)
5.	Log-log method (Robinson, 2009)	Table	3. Standardized methods used to determine the
6.	Steepest tangent fitting method (Vinod et al., 2010)	vertic	al coefficient of consolidation, <i>c_v</i>
7.	Log t method Sridhar & (Sridhar and Robinson, 2011)	1.	Log t method (Casagrande and Fadum, 1940)
8.	Full-match method (Chung et al., 2017)	2.	Root t method (Taylor, 1942)

Table 4. Methods to determine compression index (C_c), recompression index (C_r) and preconsolidation stress (σ'_p) from Oedometer test

1. Casagrande (1936)'s method

2. Silva (1970)'s method

4. Location of the Study sites

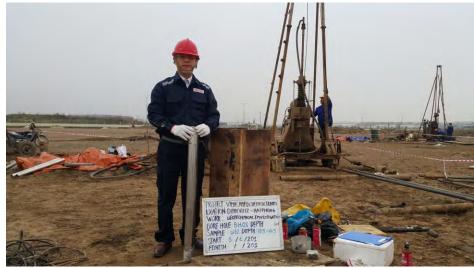


Study sites for this research were taken from supervisor's research projects. They are:

- 1. Kim Chung Residential Complex (KC)
- 2. Dinh Vu industrial Zone (DVIZ)
- 3. Vietnam Singapore Industrial Park (VSIP)
- 4. Nam Dinh Thermal Power Project (TPP)

5. Sample Collections

5.2. Field tests



Example of soil boring and sampling at DVIZ site



At each test site, soil boring and sampling were performed to collect soil samples for laboratory test. In addition, a CPTu sounding was also performed adjacent to the borehole (*carried out by the supervisor*).

- ✓ For soil boring and sampling, the borehole was advanced by using the rotary wash method with the use of bentonite slurry to stabilize the borehole walls.
- At a sampling depth, a thin-walled fixed-piston tube sampler of 1.0 m long and 76 mm in inner diameter was hydraulically pushed down to collect undisturbed clay samples.
- ✓ Right after the sample tube was retrieved at the ground surface, the tube ends were cleaned and filled with paraffin and then carefully sealed by tape to preserve water content as well as integrity of the soil sample. All the boring and sampling procedures were carried out in accordance with ASTM D1452–09 and ASTM D1587–09, respectively.
- When the sampling at the borehole was finished, the sample tubes were then carefully transported to the laboratory for lab tests

Example of performance of CPTu test at DVIZ site

5. Sample Collections

5.3. Laboratory tests

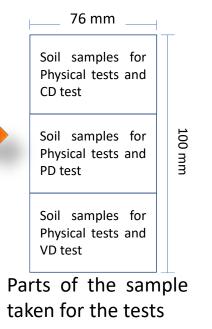


in the lab

Sample tubes stored



Sample cutting in the lab



Physical tests, i.e., water content, specific gravity...

Consolidation tests with radial drainage (CD, PD, VD)

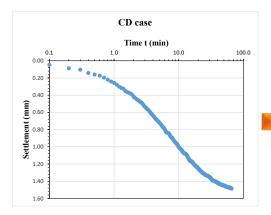
This central drain was manufactured so that the theoretical consolidation curves from a CD test and PD test are the same ($n = D_e/D_c = 2.05$).

Actual manufactured ratio: $n = \frac{62}{28} = 2.214$ (some difference due to water jet cutting error)

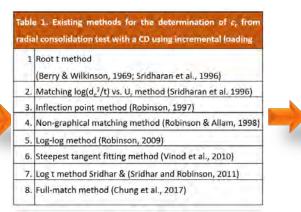


Performing the radial consolidation test in the lab

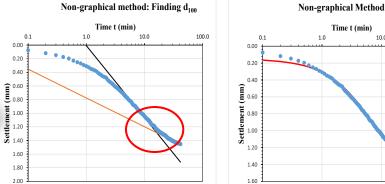
6.1. From implementation of the 1st objective Procedure for getting c_r values



Consolidation curves obtained from the radial consolidation tests in lab (CD)



Methods mentioned in slide No. 5



Time t (min) 100.0 10.0

Exampl from Non-grphical method for analyaing in Excel to get c_r

	Sample name	Method name	Pressure (kPa)	d _o (mm)	d ₁₀₀ (mm)	C _r (mm²/min)	SSD	MAPE
	KC-18 (M 31)-CD800	Root t	800	0.095	0.812	36.829	0.010	1.504
KC-18 (M 31)	KC-18 (M 31)-CD800	Log (de2/t)	800	0.074	0.837	37.000	0.003	0.759
	KC-18 (M 31)-CD800	Inflection Point	800	0.074	0.791	33.019	0.052	1.939
(23.9-24.0) m	KC-18 (M 31)-CD800	Non-graphical	800	0.074	0.837	35.788	0.003	0.750
CD	KC-18 (M 31)-CD800	Log-Log	800	0.067	1.122	27.645	0.683	4.531
	KC-18 (M 31)-CD800	Steepest tangent	800	0.031	0.837	49.832	0.045	1.946
	KC-18 (M 31)-CD800	Log t	800	0.067	0.854	36.209	0.007	0.754
	KC-18 (M 31)-CD800	Full-match	800	0.079	0.771	33.945	0.004	0.917

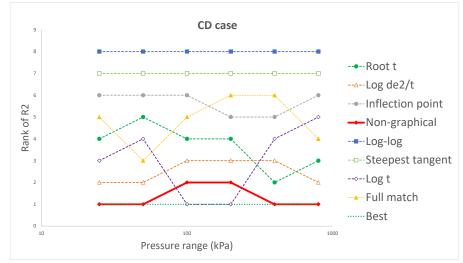
6.1. From implementation of the 1st objective Ranking the methods

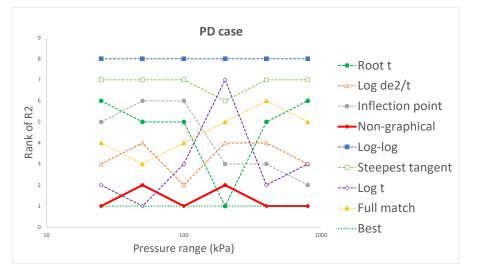
Procedures for ranking the methods (or procedures for choosing method which yield the predicted settlement results closest to the reality)

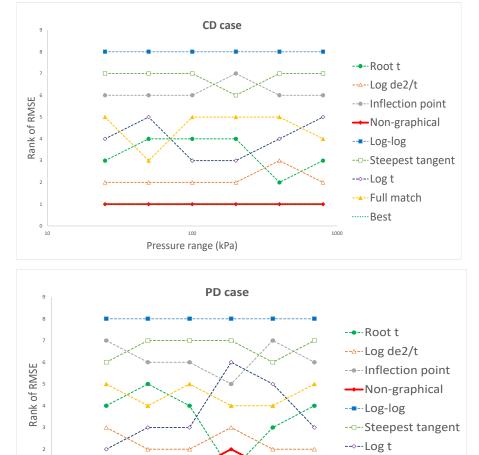
- 1. For each method, determine $c_{r,CD}$ (or $c_{r,PD}$) from the time (t) and measured settlement (δ_m) data curve (as mentioned in slide No.19 and 20).
- 2. For each method, calculate the estimated settlement of the sample (δ_e) by using the theoretical consolidation equation with the inputs of c_r , d_0 , d_{100} .
- 3. For each method, plot a graph of $\delta_m vs \delta_e$ for all data points (of one pressure level) from the 4 test sites (VSIP site, DVIZ site, KC site, TPP) and determine R^2 and Root Mean Squared Error (*RMSE*) from the correlation.
- 4. Rank the methods using R^2 and RMSE indicators. The ranking principles are as follows:
 - The higher the R² value, the better the method. Thus, the method producing the highest R² value is the best method (Rank = 1) and vice versa
 - The lower the RMSE value, the better the method. Thus, the method producing the smallest RMSE value is the best method (Rank = 1) and vice versa

6.1. From implementation of the 1st objective Ranking the methods

Ranked position of the methods based on R² and RMSE values (Intact samples)







100

Pressure range (kPa)

10

-----Full match

······Best

1000

6.1. From implementation of the 1st objective **Ranking the methods**

Ranked position of the methods based on R² and RMSE values (Intact samples)

CD case

PD case

No.	Method Name	Reliability Rank	
1.	Non-graphical method	Highest	
2.	Matching Log <i>de²/t</i> vs U _r method		
3.	Root t method		
4.	Log t method Middle		
5.	Full-match method		
6.	Inflection point method		
7.	Steepest tangent method	Lowest	
8.	Log-log method		

No.	Method Name	Reliability Rank	
1.	Non-graphical method	Highest	
2.	Matching Log <i>de²/t</i> vs U _r method		
3.	Root t method		
4.	Log t method	Middle	
5.	Full-match method		
6.	Inflection point method		
7.	Steepest tangent method	Lowest	
8.	Log-log method	2011001	

Similar result was found on remolded samples.

6.2. From implementation of the 2nd objective

Ratio of $c_{r,PD} / c_{r,CD}$ from analytical solution

Theoretical equations for PD case (Barron, 1948)

 $U_r = 1 - exp(-32T_r)$

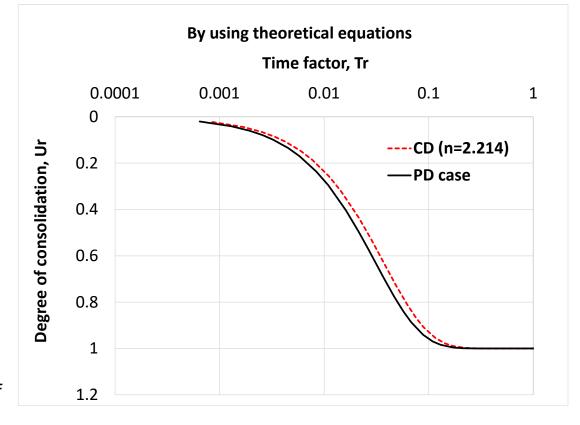
Theoretical equations for CD case (Scott, 1963)

$$U_r = 1 - exp(-\frac{8}{F(n)}T_r)$$

$$F(n) = \frac{n^2}{(n^2 - 1)}\ln(n) - \frac{(3n^2 - 1)}{4n^2}$$

$$T_r = \frac{C_r t}{D^2}$$

Where, U_r = degree of consolidation; T_r = time factor; n = drainage spacing ratio; D = diameter of soil sample



The theoretical curves at n = 2.214 indicate that the two tests (i.e., CD and PD) should result in very similar c_r values (cr,PD/cr,CD ≈ 1.0).

6.2. From implementation of the 2nd objective

Correlation between $c_{r,PD}$ and $c_{r,CD}$

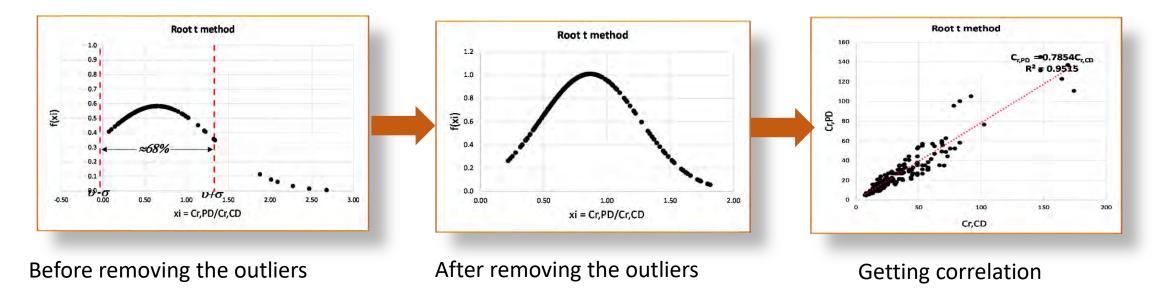
Procedures for the evaluation of correlations

- 1) For each method, determine the ratio of $c_{r,CD}$ and $c_{r,PD}$, or $c_{r,CD}$ and c_v , or $c_{r,PD}$ and c_v for both *Intact and Remolded samples*.
- 2) Plot a *normal distribution curve* by using the probability density function of a normal random variable with mean (μ) and variance (σ^2) as the y-axis and $c_{r,CD}/c_{r,PD}$, or $c_{r,CD}/c_v$, or $c_{r,CD}/c_v$ as the x-axis.
- 3) Filtering the outliers $(c_{r,CD}/c_{r,PD})$, or $c_{r,CD}/c_v$, or $c_{r,CD}/c_v$) which are out of **the 68% interval area distribution**. In other words, remove the data less than $(\mu \sigma)$ for the lower boundary and greater than $(\mu + \sigma)$ for the upper boundary.
- 4) Plot ($c_{r,CD}$ vs $c_{r,PD}$) graph with the filtered data.

6.2. From implementation of the 2nd objective

Ratio of $c_{r,PD}/c_{r,CD}$ from experimental results

Correlation between $c_{r,PD}$ and $c_{r,CD}$ for the eight methods (*Intact samples*) Example of correlation between $c_{r,PD}$ and $c_{r,CD}$ from Root t method (*Intact samples*)



6.2. From implementation of the 2nd objective

Ratio of $c_{r,PD}/c_{r,CD}$ from experimental results

No.	Method names		C _{r,PD} VS C _{r,CD}	
NU.	Method hames	R^2	$\alpha(y=\alpha x)$	No. of data point
1.	Root t	0.9515	0.7854	148
2.	Log (de²/t)	0.9332	0.708	179
3.	Inflection Point	0.9065	0.6943	214
4.	Non-graphical	0.9237	0.6705	204
5.	Log-Log	0.9212	0.6998	194
6.	Steepest tangent	0.8791	0.769	233
7.	Log t	0.8992	0.7663	189
8.	Full-match	0.9336	0.685	161

Correlation between $c_{r,PD}$ and $c_{r,CD}$ for Intact samples: $c_{r,PD} \approx (0.6 - 0.8) c_{r,CD}$

Correlation between $c_{r,PD}$ and $c_{r,CD}$ for Remolded samples: $c_{r,PD} \approx (0.4 - 0.6) c_{r,CD}$

6.2. From implementation of the 2nd objective

Ratio of $c_{r,PD}/c_v$ from experimental results

Summary table for the correlation results between $c_{r,PD}$ and c_v for the two standardized methods (Intact samples)

No.	Mathad names		c _{r,PD} Vs c _v	
INO.	Method names	R^2	α (y= α x)	No. of data point
1.	Root t	0.6205	1.2446	396
2.	Log t	0.6652	1.7926	388

Correlation between $c_{r,PD}$ and c_v for *Intact Samples*: $c_{r,PD} \approx (1-2) c_v$

Summary table for the correlation results between $c_{r,PD}$ and c_v for the two standardized methods (Remolded samples)

No	Mathad	$c_{r,PD} Vs c_{v}$			
No.	Method names	R^2	α (y= α x)	No. of data point	
1.	Root t	0.9505	0.6251	17	
2.	Log t	0.8616	0.7113	20	

Correlation between $c_{r,PD}$ and c_v for *Remolded Samples*: $c_{r,PD} \approx (0.5 - 1) c_v$

6.2. From implementation of the 2nd objective

Ratio of $c_{r,CD}/c_v$ from experimental results

Summary table for the correlation results between $c_{r,CD}$ and c_v for the two standardized methods (Intact samples)

No	Method names	$c_{r,CD}$ Vs c_v			
No.	wiethou names	R^2	α (y= α x)	No. of data point	
1.	Root t	0.7021	2.3249	344	
2.	Log t	0.6914	2.7567	348	

Correlation between $c_{r,PD}$ and c_v for Intact Samples: $c_{r,CD} \approx (2-3) c_v$

Summary table for the correlation results between $c_{r,CD}$ and c_v for the two standardized methods (Remolded samples)

No.	Method names	$c_{r,CD}$ Vs c_v			
NO.	Method hames	R^2	α (y= α x)	No. of data point	
1.	Root t	0.8304	1.6278	25	
2.	Log t	0.9018	1.7782	23	

Correlation between $c_{r,PD}$ and c_v for *Remolded Samples*: $c_{r,CD} \approx (1-2) c_v$

6.2. From implementation of the 2nd objective

Numerical analysis

Finding influent facts that cause the correlation between $c_{r,PD}$ and $c_{r,CD}$ is not equal to one.

Steps performed under the numerical analysis

1) Construct a soil model in *PLAXIS* software with the dimension of (60 mm x 20 mm) by inputting typical required parameters for soft clay as mentioned in *Table 1a and 1b* from Appendix.

• For CD case, by installing sand-stone in the middle with different *n* values (*slide 28*).

2) Apply pressure by inputting various permeability rate in horizontal direction (i.e., $k_x = k_y$, $2k_y$, $3k_y$, $4k_y$, $5k_y$) in order to see the variation in correlation between $c_{r,PD}$ and $c_{r,CD}$ is whether due to changes in coefficient of permeability in horizontal direction or not.

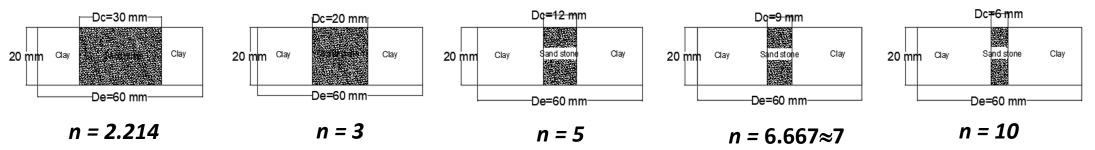
3) Find $c_{r,CD}$ with different *n* values (i.e., *n* = 2.214, 3, 5, 7, 10) as shown in slide no.28 at $k_x = 3k_y$ condition (typical case) by analyzing the results obtained from *PLAXIS* software with Root t method.

4) Find $c_{r,PD}$ as well by analyzing the results obtained from *PLAXIS* software with Root t method.

6.2. From implementation of the 2nd objective

Numerical analysis

Configuration of variation in sand drain ratio $(n=D_e/D_c)$ for CD case (Numerical Analysis)



Configuration of sand-stone position in PD case (Numerical Analysis)



Example of soil domain from *PLAXIS* software (CD case, 10 kPa, $k_x = 3k_y$)

6.2. From implementation of the 2nd objective

Numerical analysis

Finding influent facts that cause the correlation between $c_{r,PD}$ and $c_{r,CD}$ is not equal to one.

Summary table for the correlation results between $c_{r,PD}$ and $c_{r,CD}$ by using Root t method (10 kPa).				
<i>k_x</i> (m/day)	<i>k_y</i> (m/day)	<i>c_{r,CD}</i> (mm²/min), <i>n</i> =2.14 case	<i>c_{r,PD}</i> (mm²/min)	C _{r,PD} ∕C _{r,CD}
k	k	2.074	1.632	0.79
2k	k	4.296	3.345	0.78
3k	k	6.247	4.730	0.76
4k	k	8.024	6.324	0.79
5k	k	9.906	7.973	0.80

Correlation between $c_{r,PD}$ and $c_{r,CD}$ from numerical analysis: $c_{r,PD} \approx (0.7 - 0.8) c_{r,CD}$

The correlation results from Intact samples and Numerical analysis are almost the same.

6.2. From implementation of the 2nd objective

Numerical analysis

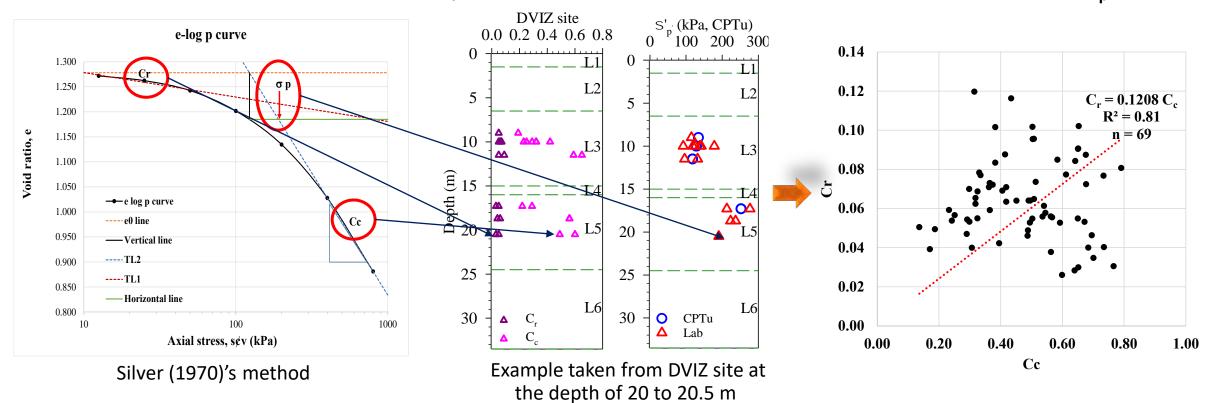
Finding influent facts that cause the correlation between $c_{r,PD}$ and $c_{r,CD}$ is not equal to one.

Table showing the variation in $c_{r,CD}$ and $c_{r,PD}/c_{r,CD}$ results based on different <i>n</i> values (10 kPa).					
k_x (m/day)	<i>k_y</i> (m/day)	n (D _e /D _c)	c _{r,CD} (mm²/min)	<i>c_{r,PD}</i> (mm²/min)	C _{r,PD} / C _{r,CD}
3 <i>k</i>	k	2.214	6.25	4.730	0.76
3 <i>k</i>	k	3	4.30	4.730	1.1
3 <i>k</i>	k	5	1.88	4.730	2.52
3 <i>k</i>	k	6.667≈7	1.00	4.730	4.73
3 <i>k</i>	k	10	0.72	4.730	6.57

The results from numerical analysis are showing that the correlation ratio $(c_{r,PD}/c_{r,CD})$ was found to be highly influenced by n values (i.e., D_e/D_c). In other words, the drainage length has a high influent effect on the results of correlation ratio $(c_{r,PD}/c_{r,CD})$.

6.3. From implementation of the 3rd objective

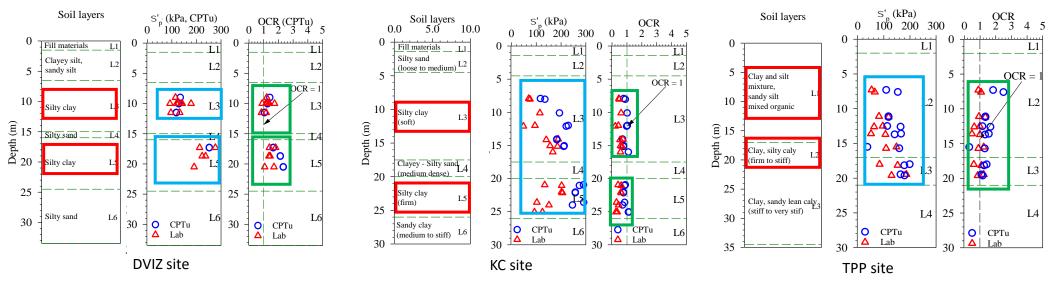
Evaluation of compression index (C_c), recompression index (C_r) and preconsolidation stress (σ'_p)

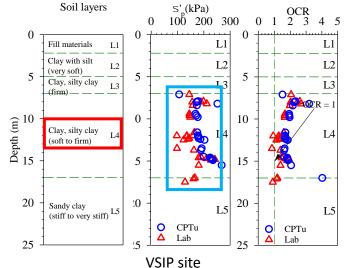


Summary table for the correlation results between C_c and e_0 and C_r and C_c						
Correlation R ² No. of data poi						
$C_c = 0.3864 \ e_0$	0.9475	69				
$C_r = 0.1208 C_c$	0.81	69				

6.3. From implementation of the 3rd objective

Evaluation of compression index (C_c), recompression index (C_r) and preconsolidation stress (σ'_p)





- In general, the OCR profiles indicate that the clays at the test sites are normally consolidated (OCR ≈ 1)
- ▶ Preconsolidation stress value (σ'_p) from Lab test is typically smaller than that from CPTu test. This indicate that the σ'_p from lab test is influence from soil disturbance effect.

7. Conclusions

Based on the results obtained from the four study sites, some key findings on the compressibility characteristics of soft clay from RRD can be highlighted as follows:

1. For the 1st objective

c_{r,PD} and c_{r,CD} values were determined from 8 existing methods. The results indicate that Non-graphical results in highest reliability and the Log-log and Steepest tangent methods result in lowest reliability. In addition, the reliability of the methods also depends on applied pressure.

2. For the 2nd objective

- Theoretically, the ratio $(c_{r,PD}/c_{r,CD})$ from analytical solution (at n = 2.214) is approximately 1.0. Experimental results from intact soil samples show that $c_{r,PD} = (0.6 - 0.8)c_{r,CD}$ and from remolded sample $c_{r,PD} \approx (0.4 - 0.6) c_{r,CD}$. These results indicate that the drainage length of actual soil has significant influence to the ratio \rightarrow for the same soil sample the test with different n value would give different $c_{r,CD}$ value.
- Results from numerical study (with n = 2.214) show that $c_{r,PD} = 0.76c_{r,CD}$, which agree well with the experimental results.

3. For the 3rd objective

• The OCR from laboratory test and CPTu test indicate that the soft clays at the test sites are predominantly normally consolidated (i.e., OCR \approx 1.0). Primary correlations of $C_c = 0.3864 e_0$ and $C_r = 0.1208 C_c$ could be suggested for the clays at the test sites.

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