

SDM8/9 - THEORY, MEASUREMENT AND MODELLING OF DAMPING FOR SEISMIC RESPONSE ANALYSIS OF LARGE-SCALE STRUCTURES

MONITOR 24

# IDENTIFICATION OF DYNAMIC CHARACTERISTICS FOR STEEL ARCH BRIDGE BY SEISMIC OBSERVATION RECORDS

ISHII Yosuke<sup>1</sup>, NAKAO Yoshihiro<sup>2</sup> and SHOJI Gaku<sup>3</sup>

<sup>1</sup>Earthquake Disaster Management Division, NILIM, MLIT, Japan, Ph. D. (Eng.)

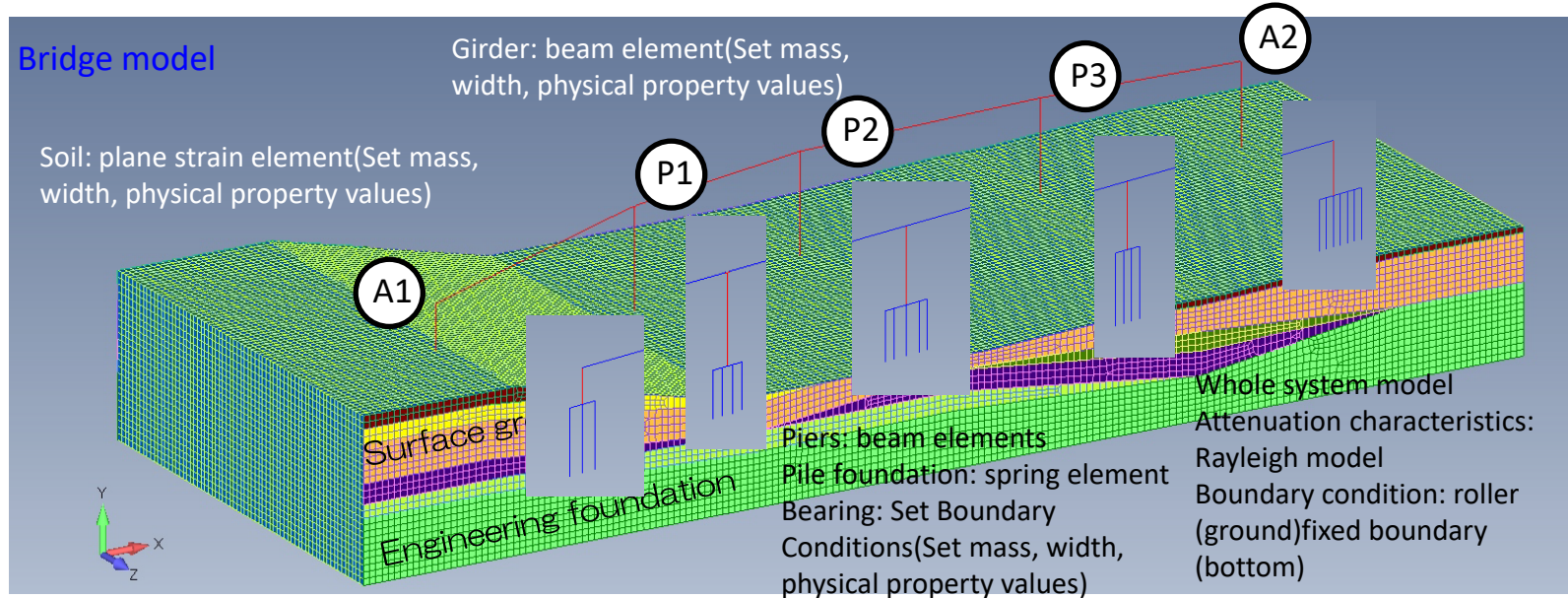
<sup>2</sup>Head of Earthquake Disaster Management Division, NILIM, MLIT, Japan (At the time of the research)

<sup>3</sup>Professor, Faculty of Engineering, Information and Systems, University of Tsukuba, Japan, Dr. Eng

- A bridge is a composite structural system consisting of members such as girders, piers, foundations, and the ground.
- Road bridge models are complex due to the inclusion of various elements.

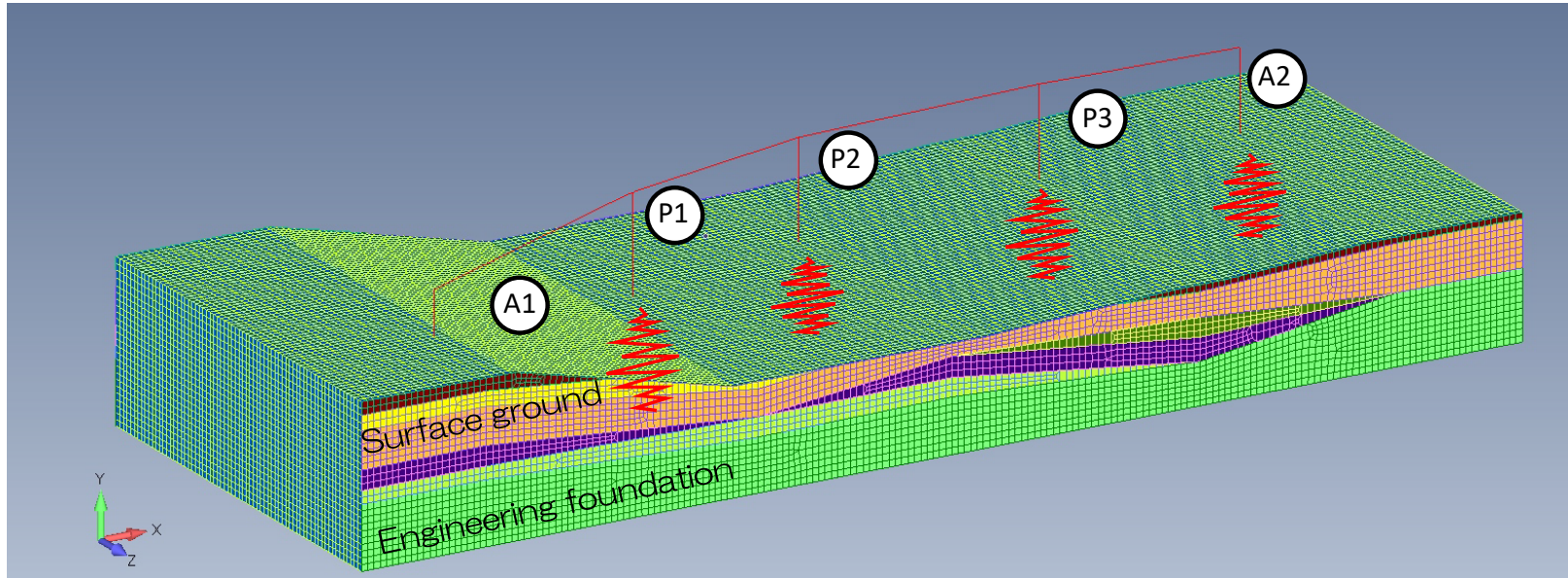


- ✓ Bridge structure-ground system includes various natural frequencies, damping characteristics, and boundary conditions.

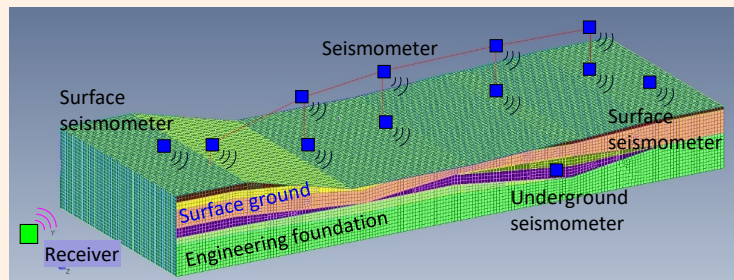


## *Introduction; Importance of understanding the vibration characteristics of bridges*

- Road bridges are affected by stationary external forces such as traffic vibrations and unsteady external forces such as seismic ground motion.
- The vibration phenomenon (input-output relationship) of road bridges is difficult to quantitatively understand.
- Vibration of road bridges is excited by the characteristics of external forces.
- ✓ **Need to understand vibration characteristics of bridges by vibration observation.**



## Development of the strong motion monitoring system "SMMS"



→ Y. Ishii, Y. Nakao, G. Shoji: *EVACES 2023, LNCE, volume 433, pp. 479–489, 2023.*

## Observation of bridge structure-ground system vibration records

### Waveform processing

- Identification of dominant frequency

### Comparison

### System identification

- Evaluation of natural frequencies, damping characteristics, and vibration modes of bridge structure-ground systems

### Comparison

### Modeling

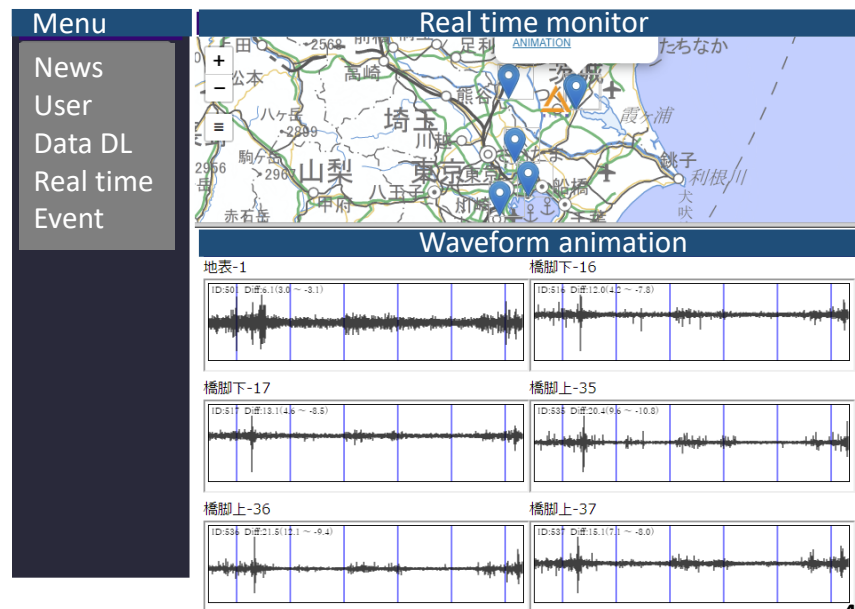
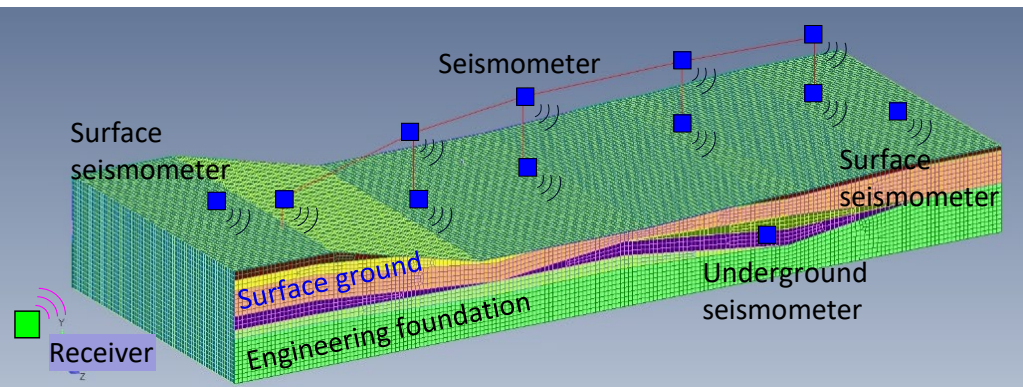
- Estimation of natural vibration mode of analytical model
- Verification of damping characteristics

Identification of vibration mode of target bridge by combining multiple methods



→ Y. Ishij, Y. Nakao, G. Shoji: Estimation of vibration characteristics for a bridge-underground system by subspace model identification method using multi-point monitoring seismic records, EVACES 2023, LNCE, volume 433, pp. 479–489, 2023.

- Transmission of observation data by wireless communication.
- The seismometer is always working. → **SMMS enables continuous vibration observation.**



# Strong Motion Monitoring System

→ Y. Ishii, Y. Nakao, G. Shoji: *EVACES 2023, LNCE, volume 433, pp. 479–489, 2023.*

- Installed on road bridges of various structure types designed according to Japanese seismic design standards.



e.g. Girder bridge



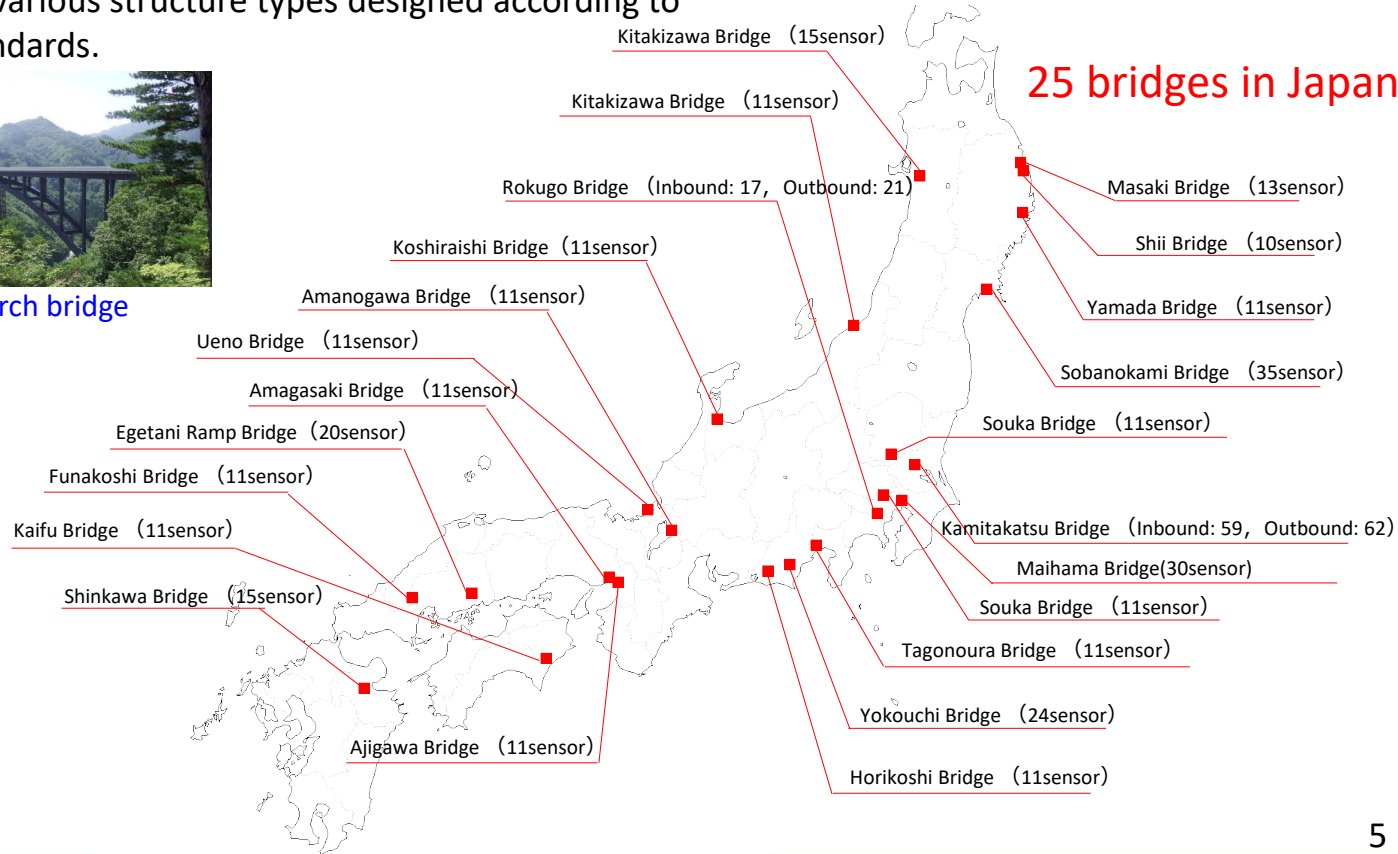
e.g. Arch bridge



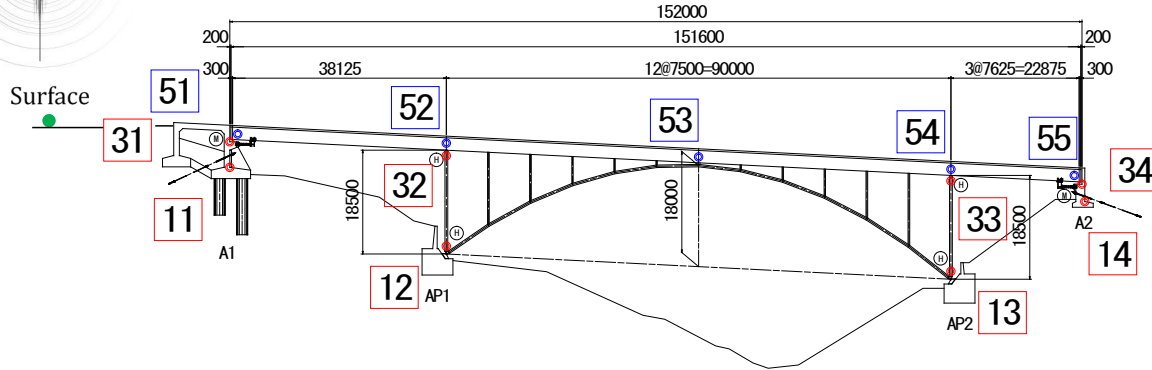
e.g. Damping device



Sensor installation status



## Case study of SMMS for applying a bridge



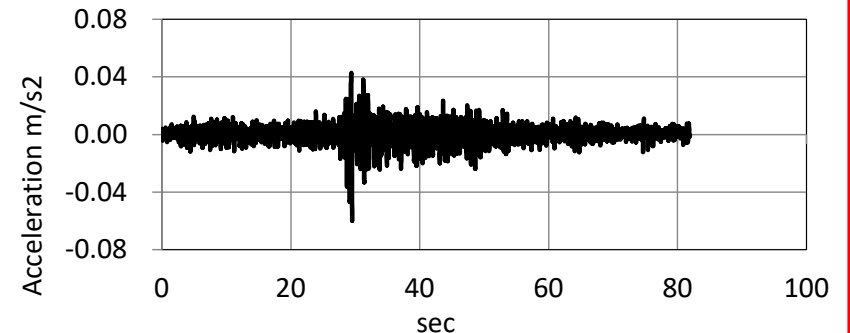
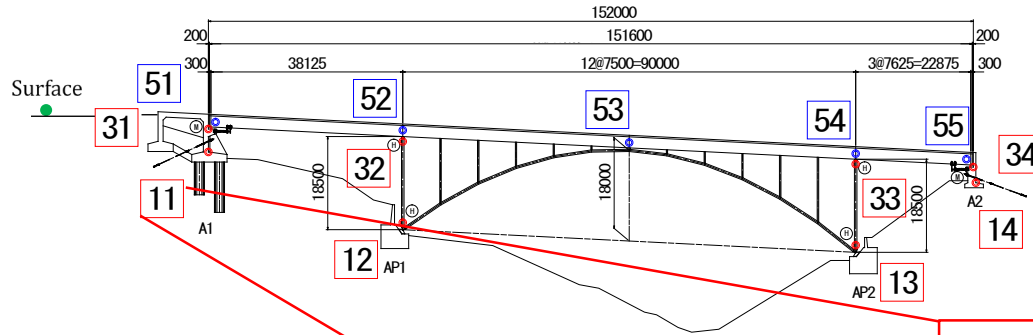
Target bridge and SMMS installation location

Specifications of the target bridge

|                |                                                            |
|----------------|------------------------------------------------------------|
| Bridge length  | 152.0m                                                     |
| Span length    | 38.125m + 90.000m + 22.875m                                |
| Superstructure | 3-span continuous steel arch girder (steel reverse langer) |
| Substructure   | Inverted T-shaped abutment                                 |
| Foundation     | Deep foundation pile, direct foundation                    |
| Ground type    | Type I ground                                              |

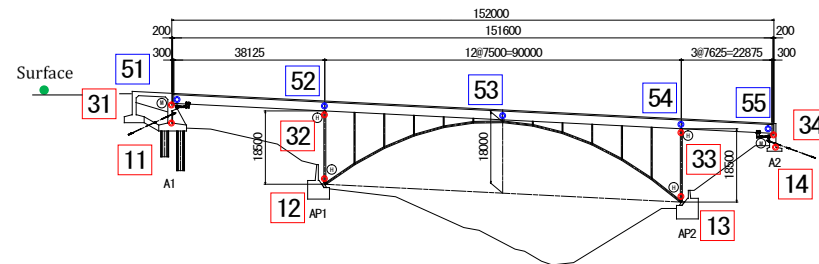
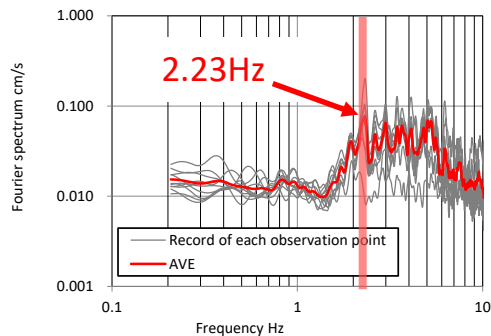


- Observation of earthquake off the coast of Fukushima Prefecture on March 16, 2022  
 → Seismic intensity of about 2 on the target bridge
- The waveform was cut out 30 seconds from the start of the earthquake and 50 seconds from the end of the earthquake.

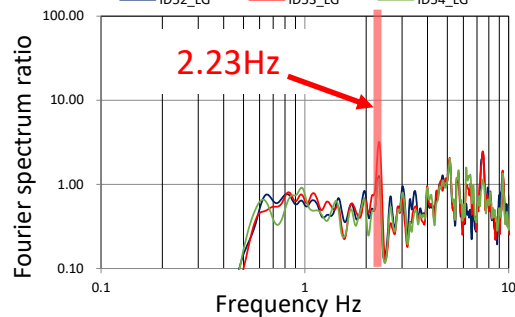




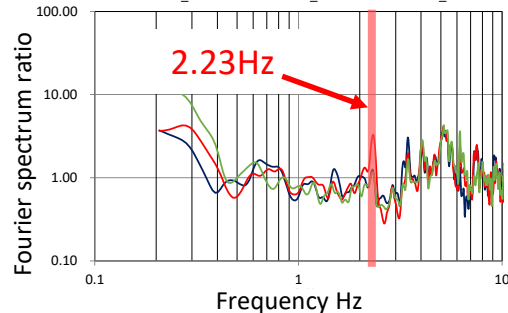
# Fourier Spectral Ratio for the LG direction



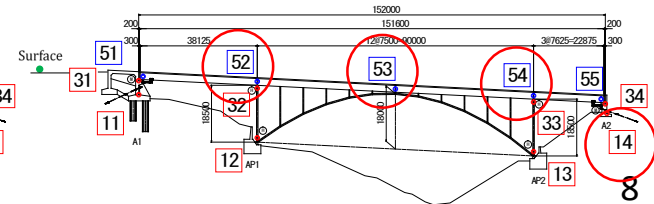
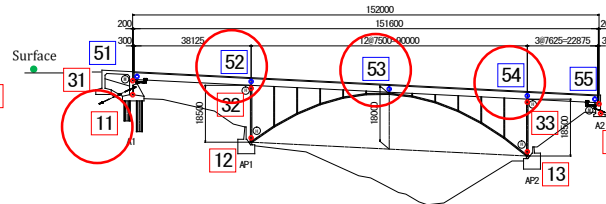
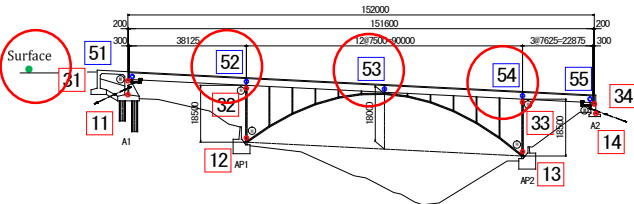
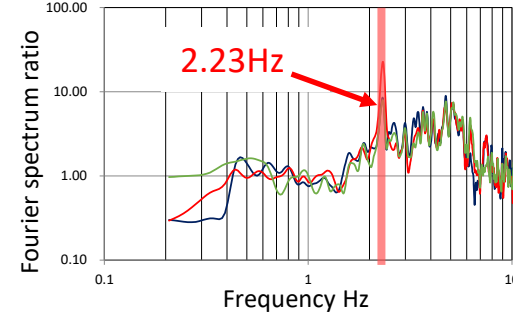
Ground surface - girder



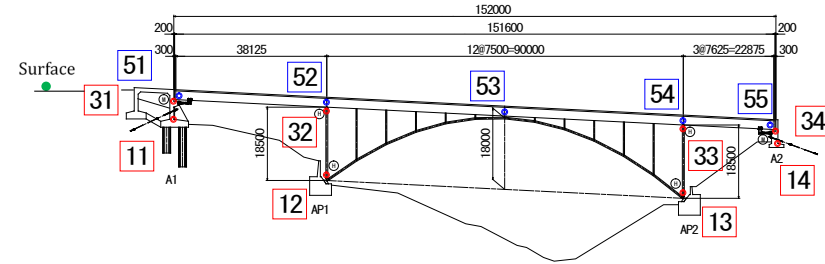
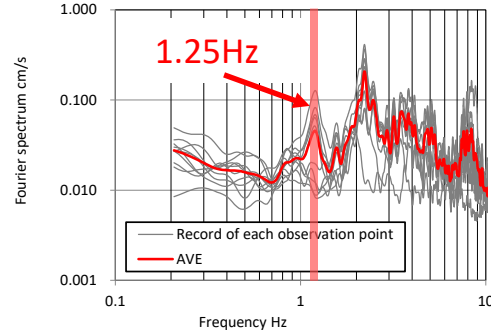
A1 abutment base - girder



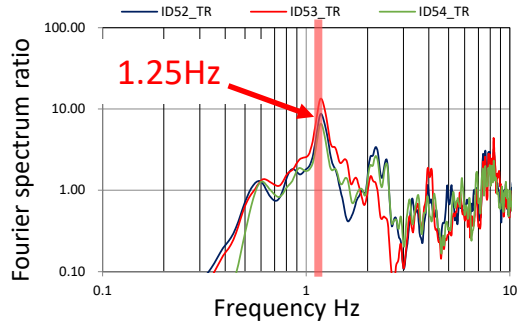
A2 abutment base - girder



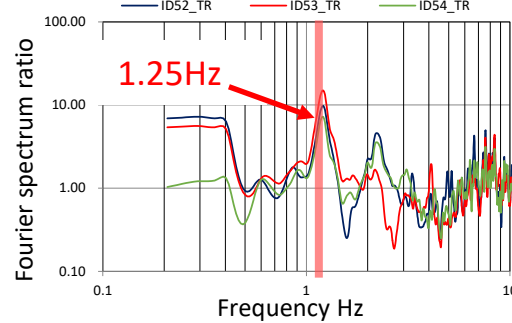
## Fourier Spectral Ratio for the TR direction



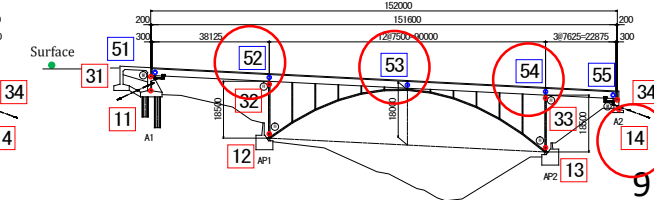
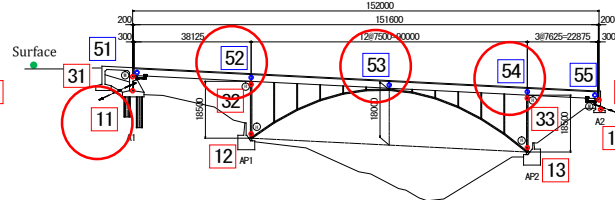
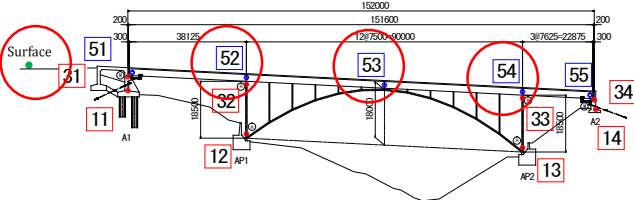
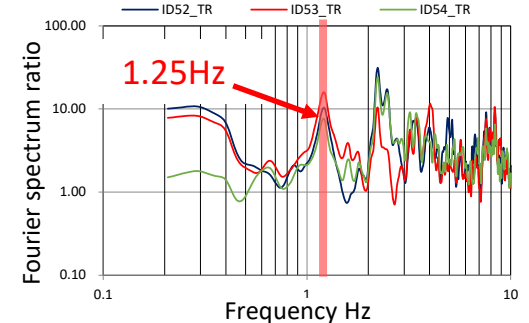
Ground surface - girder



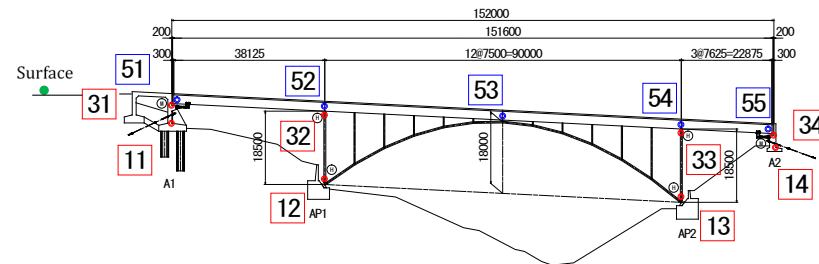
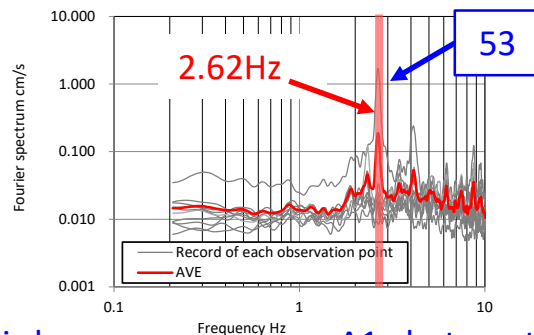
A1 abutment base - girder



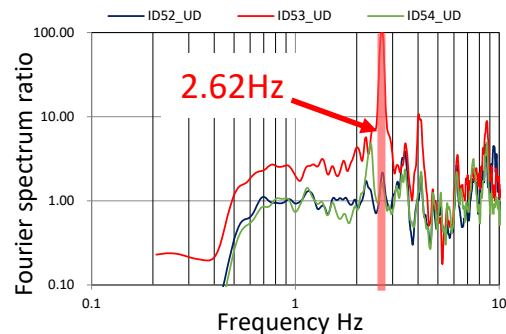
A2 abutment base - girder



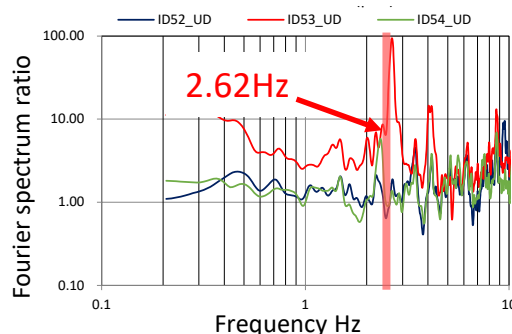
# Fourier Spectral Ratio for the Vertical direction



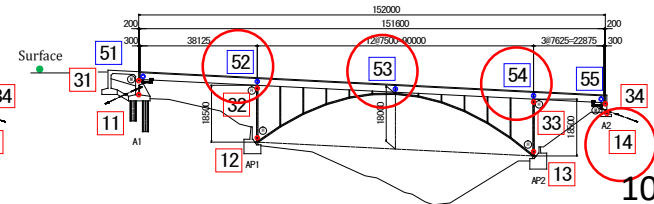
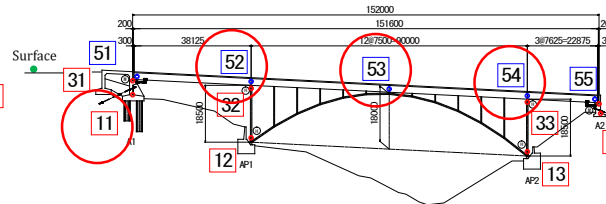
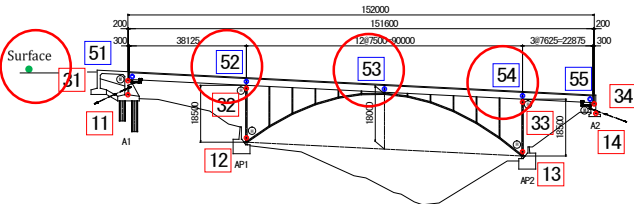
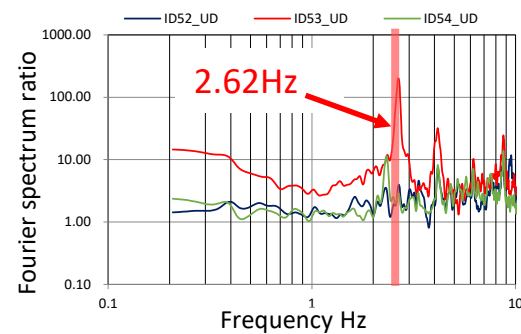
Ground surface - girder



A1 abutment base - girder

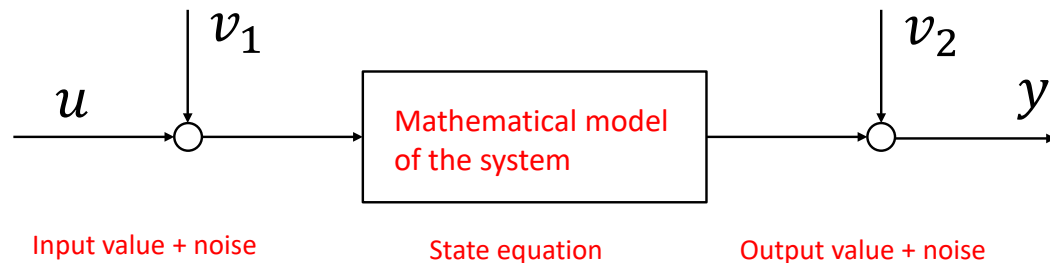
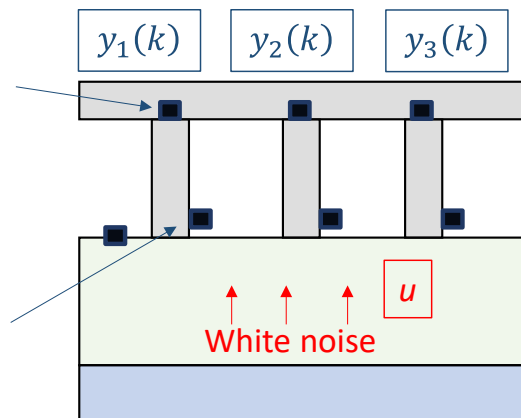


A2 abutment base - girder



- **The Ordinary MOESP method**; Ordinary Multi variable Output-Error State sSpace method using input and output was proposed by Verhaegen *et al.* (1992).
- **The SSI-COV method**; COVariance-driven Stochastic Subspace Identification method, which performs identification calculations using only output, was developed by Peeters (2000).

System identification (e.g.; Peeters)



Input value + noise

State equation

Output value + noise

Equation of motion

$$[M]\{\ddot{\mathbf{z}}_k\} + [\xi]\{\dot{\mathbf{z}}_k\} + [K]\{\mathbf{z}_k\} = -[M]\{1\}\{\ddot{\mathbf{u}}_{o,k}\}$$

State equation

$$\{\mathbf{x}_k\} \equiv \{\{\mathbf{z}_k\}^T \quad \{\dot{\mathbf{z}}_k\}^T\}^T$$

$$\{\mathbf{x}_{k+1}\} = [A]\{\mathbf{x}_k\} + [B]\{\ddot{\mathbf{u}}_{o,k}\}$$

Equation of output

$$\{\mathbf{y}_k\} = [C]\{\mathbf{x}_k\} + [D]\{\ddot{\mathbf{u}}_{o,k}\}$$

$[\xi]$  : Damping matrix

$\mathbf{z}_k$  : Relative displacement

$[M]$  : Mass matrix

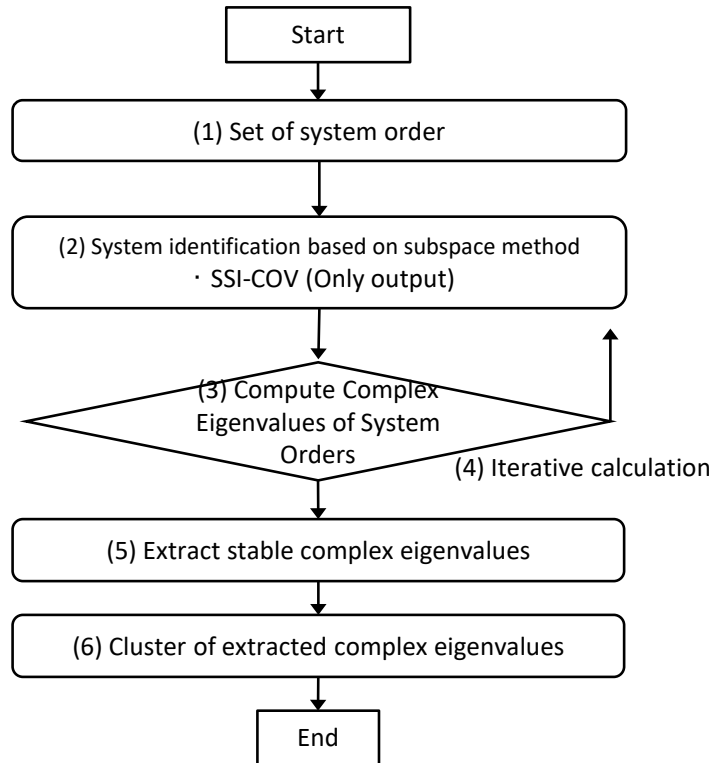
$\ddot{\mathbf{u}}_{o,k}$  : Disturbance

$[K]$  : Stiffness matrix

$k$  : Number of steps

- We estimated the natural frequency and damping characteristics of the bridge using both Ordinary MOESP and SSI-COV.

## System identification flow



## No input    Abutment base input

| Classification                       | Item description                                               | CASE1                                                                                       | CASE2                                         |
|--------------------------------------|----------------------------------------------------------------|---------------------------------------------------------------------------------------------|-----------------------------------------------|
| System identification<br>(1) ~ (4)   | Technique                                                      | SSI-COV                                                                                     | Ordinary MOESP                                |
|                                      | Time interval $\Delta t$                                       | 0.025 s                                                                                     | 0.025 s                                       |
|                                      | Number of inputs                                               | -                                                                                           | 2 points under the pier                       |
|                                      | Number of outputs                                              | 2 points under the pier<br>3 points on pier top<br>5 points girder parts<br>1 point surface | 3 points on pier top<br>5 points girder parts |
|                                      | Number of samples N                                            | 4800<br>(120s)                                                                              | 4800<br>(120s)                                |
| Complex eigenvalue extraction<br>(5) | Number of block lines M                                        | 100<br>(5.0s)                                                                               | 100<br>(5.0s)                                 |
|                                      | System order maximum n                                         | 100                                                                                         | 100                                           |
|                                      | System order Minimum n                                         | 20                                                                                          | 20                                            |
|                                      | Natural frequency Stability judgment threshold $\varepsilon_f$ | 0.01                                                                                        | 0.01                                          |
|                                      | Mode shape Stable judgment threshold $\varepsilon_\psi$        | 0.02                                                                                        | 0.02                                          |
|                                      | Upper limit of attenuation $h_{\max}$                          | 0.4                                                                                         | 0.4                                           |
| Clustering<br>(6)                    | Technique                                                      | Hierarchical clustering (group average method)                                              |                                               |

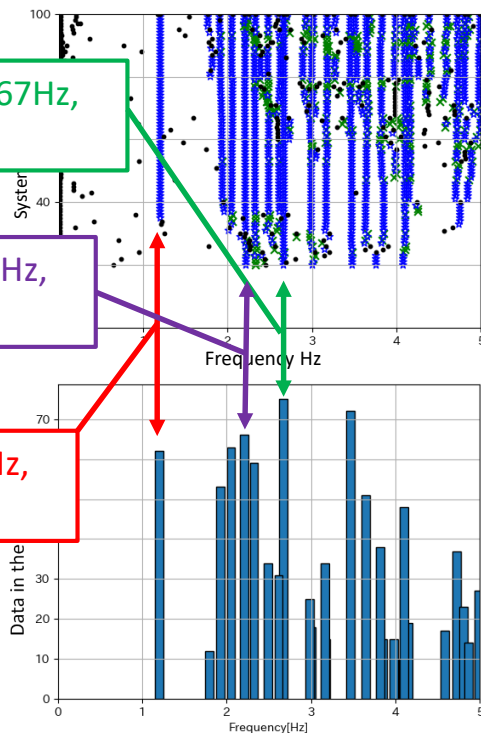


## System Identification Results for Arch Bridge

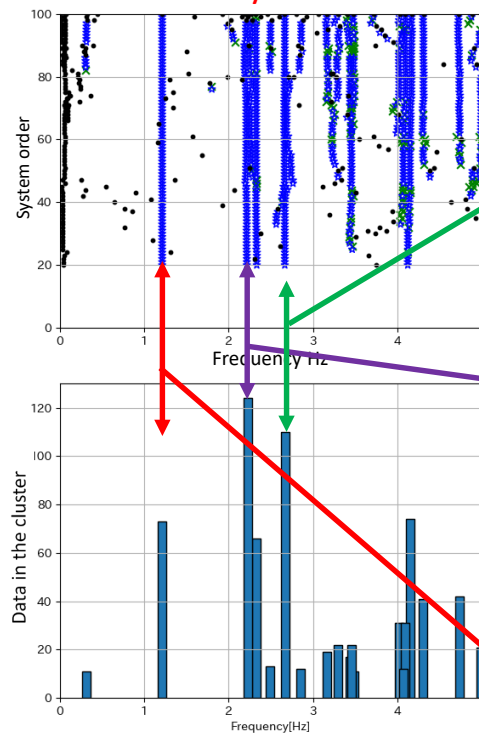
➤ Natural frequencies evaluated were around 1.20/1.21Hz, 2.21/2.23Hz, and 2.67Hz.

Stabilization diagram (top) and number of data (bottom)

SSI-COV



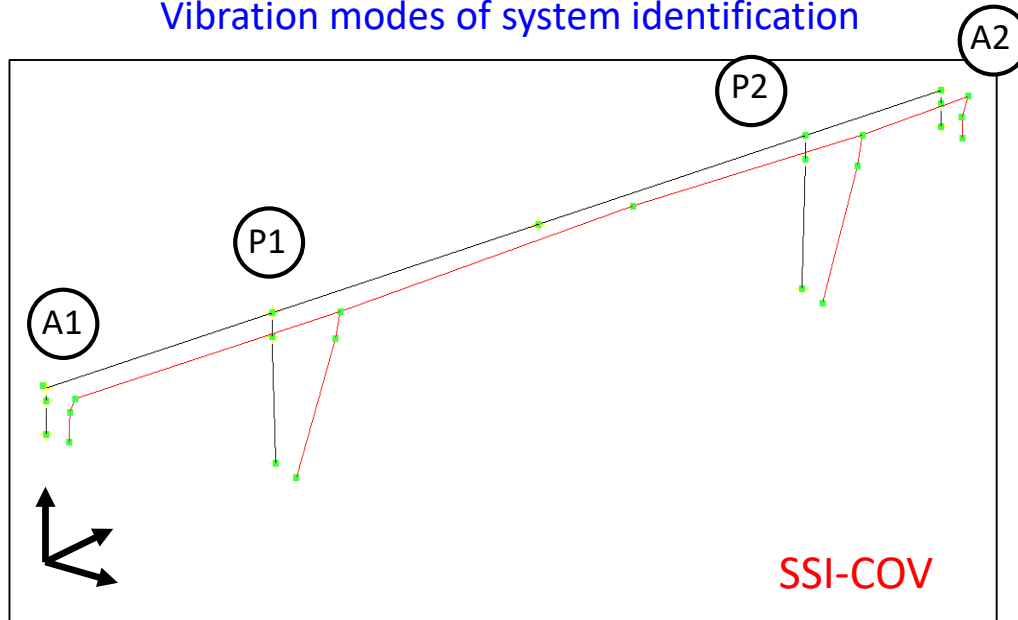
Ordinary MOESP



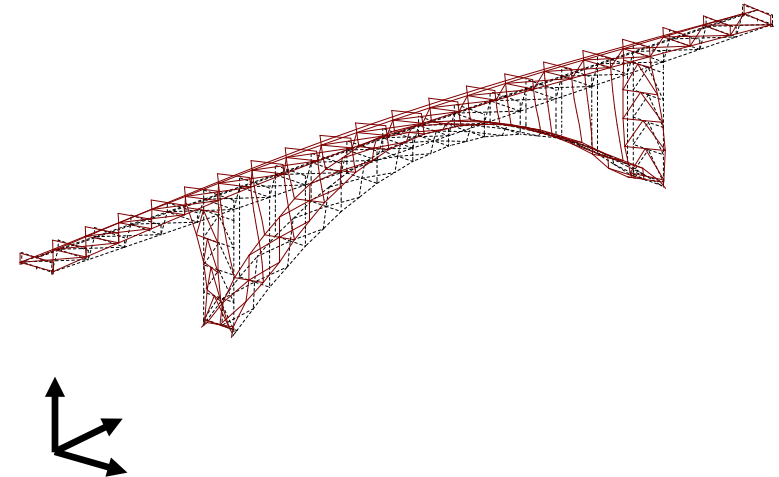
- ☆ : When there is a correlation between the natural frequency and the eigenvector
- × : When there is a correlation only with the natural frequency
- : When there is no correlation but the calculated natural frequency

- The **1.21Hz** vibration mode estimated by system identification is exerted in the bridge TR direction.  
 → Matches the dominant frequency in the bridge TR direction.
- Also matches the vibration mode obtained from the eigenvalue analysis of the target bridge.

Vibration modes of system identification

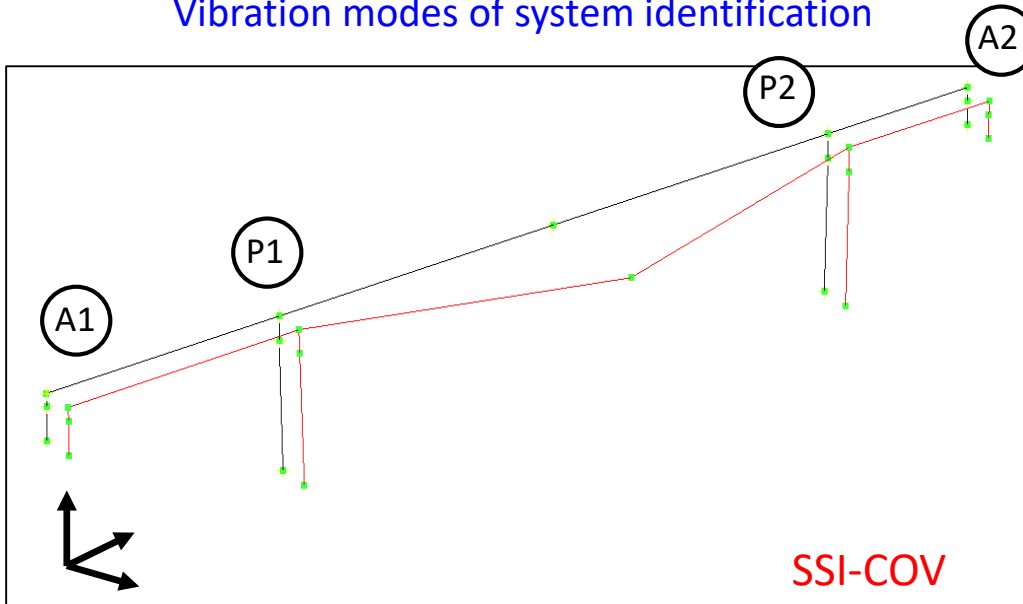


Vibration modes of eigenvalue analysis

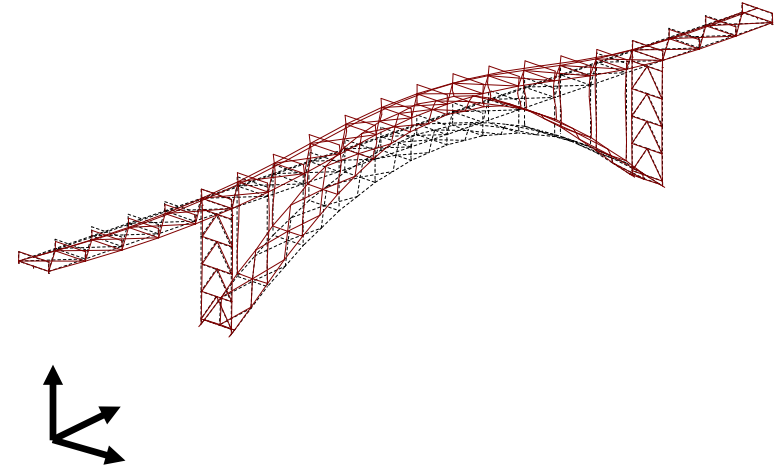


- The 2.67Hz vibration mode estimated by system identification is exerted in the vertical direction.  
 → Matches the dominant frequency in the vertical direction.
- The center of the girder has a larger response than the other observation points  
 → It is believed that this reflects the difference in response in the observation records.

Vibration modes of system identification

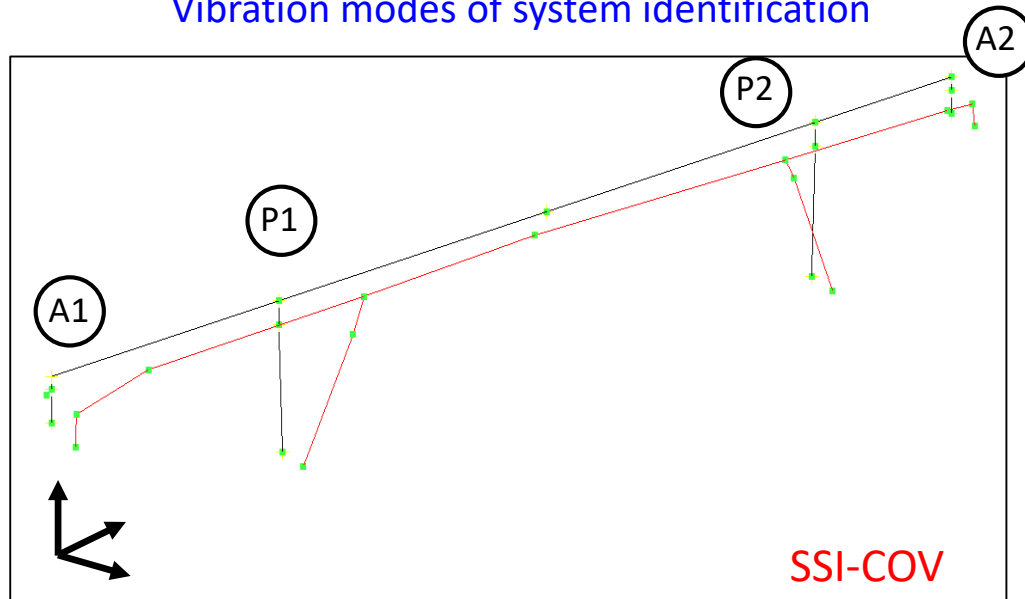


Vibration modes of eigenvalue analysis

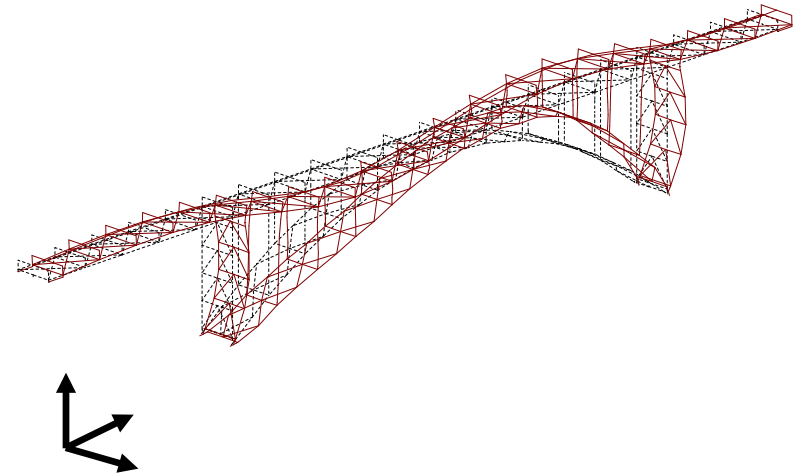


- The vibration mode of 2.23Hz estimated by system identification is a mode in which the left and right pillars are in opposite phase toward the center, and is expressed in the bridge LG direction.
- The fact that a vibration mode appeared in the bridge LG direction is consistent with the dominant frequency.

Vibration modes of system identification



Vibration modes of eigenvalue analysis



### Development of the strong motion monitoring system "SMMS"

#### Observation of vibration records of the arch bridge

##### Waveform processing

- Estimated dominant frequency  
→ **2.23Hz** in the bridge LG direction  
→ **1.21Hz** in the bridge TR direction  
→ **2.67Hz** vertical direction

##### System identification

- SSI-COV, Ordinary MOESP  
→ Evaluation of **natural frequencies**  
→ Evaluation of **damping characteristics**  
→ Evaluation of **vibration modes**

##### Modeling

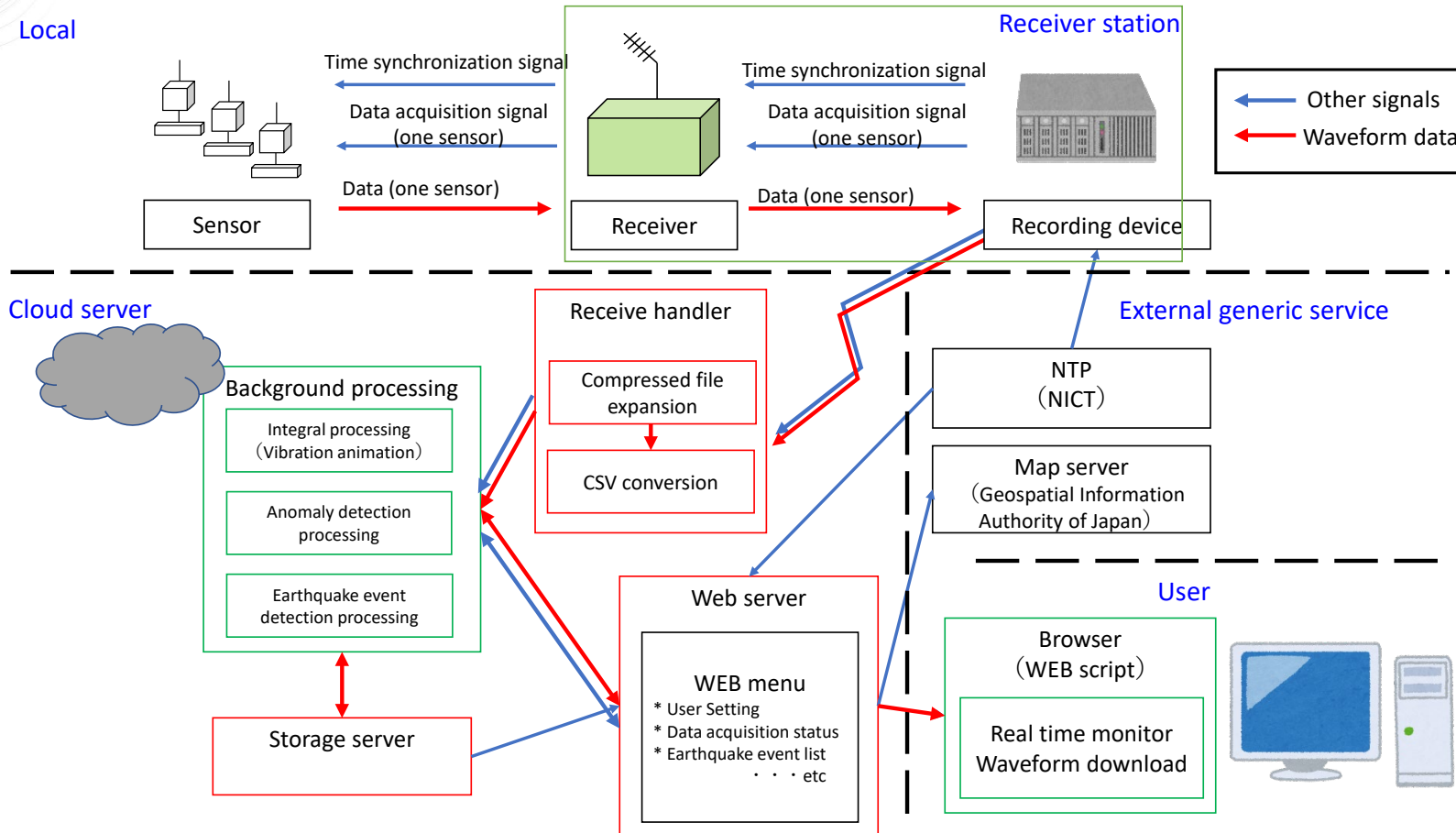
- Natural vibration modes based on analytical models  
→ Evaluation of natural frequencies

### Findings gained from the study

- ✓ The vertical observation records in the center of the arch structure showed particularly large accelerations and prominent peak amplitudes compared to other observation records.
- ✓ The vibration mode was evaluated by system identification in the TR direction and the vertical direction.
- ✓ The vibration mode in the LG direction evaluated by system identification was a vibration mode that could not be expressed by the vibration mode obtained by eigenvalue analysis of the analysis model.
- ✓ The damping characteristics estimated by system identification need to be verified by model analysis.

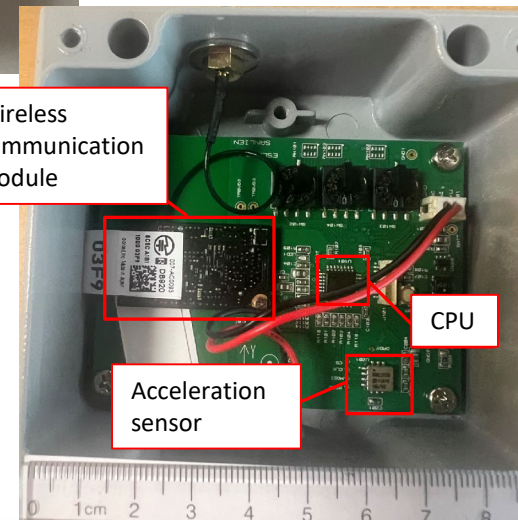
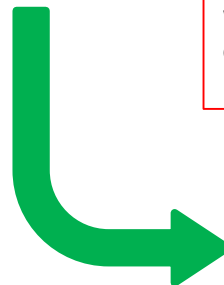
# References





## Seismometer performance

|                          |                                                        |
|--------------------------|--------------------------------------------------------|
| Sensor type              | Accelerometer                                          |
| Measurement range        | $\pm 10\text{m/s}^2$                                   |
| Resolution               | 1 mm/s <sup>2</sup>                                    |
| Measuring axis           | 3 axes (2 horizontal directions, 1 vertical direction) |
| Observation method       | 24-hour continuous observation                         |
| Data transmission method | 920MHz band wireless communication                     |
| Sampling frequency       | 100Hz                                                  |
| Waterproof performance   | IP65                                                   |
| Weight                   | 600g                                                   |
| Power supply             | Battery                                                |



## ➤ Natural frequency and mode damping

### SSI-COV: no input

| Mode order | Natural frequency      |                   | Mode damping          |                  | Data      |
|------------|------------------------|-------------------|-----------------------|------------------|-----------|
|            | $f_{\text{mean}}$ (Hz) | $f_{\sigma}$ (Hz) | $h_{\text{mean}}$ (%) | $h_{\sigma}$ (%) | $n_c$ (-) |
| 1          | 1.20                   | 0.00              | 2.63                  | 0.04             | 62        |
| 2          | 1.79                   | 0.02              | 6.32                  | 0.26             | 12        |
| 3          | 1.92                   | 0.01              | 0.56                  | 0.14             | 53        |
| 4          | 2.05                   | 0.00              | 1.06                  | 0.22             | 63        |
| 5          | 2.21                   | 0.00              | 0.70                  | 0.12             | 66        |
| 6          | 2.32                   | 0.00              | 0.52                  | 0.07             | 59        |
| 7          | 2.49                   | 0.00              | 1.93                  | 0.26             | 34        |
| 8          | 2.62                   | 0.01              | 1.53                  | 0.13             | 31        |
| 9          | 2.67                   | 0.00              | 0.20                  | 0.04             | 75        |
| 10         | 2.99                   | 0.01              | 1.58                  | 0.05             | 25        |
| 11         | 3.00                   | 0.01              | 1.26                  | 0.05             | 18        |
| 12         | 3.17                   | 0.01              | 0.32                  | 0.12             | 34        |
| 13         | 3.18                   | 0.00              | 0.27                  | 0.09             | 15        |
| 14         | 3.46                   | 0.01              | 0.76                  | 0.25             | 72        |
| 15         | 3.65                   | 0.01              | 1.17                  | 0.19             | 51        |

### Ordinary MOESP: input of abutment base

| Mode order | Natural frequency      |                   | Mode damping          |                  | Data      |
|------------|------------------------|-------------------|-----------------------|------------------|-----------|
|            | $f_{\text{mean}}$ (Hz) | $f_{\sigma}$ (Hz) | $h_{\text{mean}}$ (%) | $h_{\sigma}$ (%) | $n_c$ (-) |
| 1          | 0.31                   | 0.01              | 6.68                  | 1.45             | 11        |
| 2          | 1.21                   | 0.00              | 0.39                  | 0.03             | 73        |
| 3          | 2.23                   | 0.03              | 2.40                  | 0.59             | 124       |
| 4          | 2.33                   | 0.00              | 0.63                  | 0.03             | 66        |
| 5          | 2.49                   | 0.00              | 1.28                  | 0.46             | 13        |
| 6          | 2.67                   | 0.02              | 0.29                  | 0.14             | 110       |
| 7          | 2.85                   | 0.01              | 1.31                  | 0.14             | 12        |
| 8          | 3.17                   | 0.01              | 0.59                  | 0.14             | 19        |
| 9          | 3.29                   | 0.01              | 4.46                  | 0.63             | 22        |
| 10         | 3.44                   | 0.01              | 0.93                  | 0.05             | 17        |
| 11         | 3.45                   | 0.00              | 0.63                  | 0.10             | 22        |
| 12         | 3.48                   | 0.00              | 1.16                  | 0.09             | 11        |
| 13         | 4.02                   | 0.01              | 0.94                  | 0.66             | 31        |
| 14         | 4.07                   | 0.00              | 0.27                  | 0.03             | 12        |
| 15         | 4.09                   | 0.01              | 0.66                  | 0.03             | 31        |